Modeling Relational Event Dynamics with statnet

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Contents

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The network modeling software demonstrated in this tutorial is authored by Carter Butts (`relevent`, `sna`).

The `statnet` Project

All `statnet` packages are open-source, written for the **R** computing environment, and published on CRAN. The source repositories are hosted on GitHub. Our website is statnet.org

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Section 0. Introduction to the Tutorial

This workshop and tutorial provide an introduction to statistical modeling of relational event data using `statnet` software. This online tutorial is also designed for self-study, with example code and self-contained data. The `statnet` package we will be demonstrating is:

- `relevent` – modeling and simulation for relational event models

Additional background on the tools, modeling framework, and data used in this tutorial may be found in the references at the bottom of this document.

0.0 Prerequisites

This workshop assumes basic familiarity with **R**, experience with network concepts, terminology and data, and familiarity with the general framework for statistical modeling and inference. While previous experience with relational event models (REMs) is not required, some of the topics covered here may be difficult to understand without a strong background in linear and generalized linear models in statistics.

0.1 Software installation

Minimally, you will need to install the latest version of **R** (available here) and the `statnet` packages `relevent`, `sna` and `network` to run the code presented here (`sna` will automatically install `network` when it is installed).

The full set of installation instructions with details can be found on the `statnet` workshop wiki.

If you have not already downloaded the `statnet` packages for this workshop, the quickest way to install these (and the other most commonly used packages from the `statnet` suite), is to open an R session and type:

```r
install.packages(c("relevent","sna"))
```

```r
library(relevent)
```

```
Loading required package: trust

Loading required package: sna

Loading required package: statnet.common

Attaching package: 'statnet.common'

The following objects are masked from 'package:base':

    attr, order

Loading required package: network

'network' 1.18.1 (2023-01-24), part of the Statnet Project
* 'news(package="network")' for changes since last version
* 'citation("network")' for citation information
* 'https://statnet.org' for help, support, and other information

sna: Tools for Social Network Analysis
Version 2.7-1 created on 2023-01-24.
copyright (c) 2005, Carter T. Butts, University of California-Irvine
 For citation information, type citation("sna").
 Type help(package="sna") to get started.

Loading required package: coda

relevent: Relational Event Models
Version 1.2-1 created on 2023-01-24.
copyright (c) 2007, Carter T. Butts, University of California-
```

```
Irvine
 For citation information, type citation("relevent").
 Type help(package="relevent") to get started.
```

```r
library(sna)
```

You can check the version number with:

```r
packageVersion("relevent")
```

```
[1] '1.2.1'
```

Throughout, we will set a random seed via `set.seed()` for commands in tutorial that require simulating random values—this is not necessary, but it ensures that you will get the same results as the online tutorial.

Section 1. Dyadic Relational Event Models with `rem.dyad`: Ordinal Timing

Dyadic relational event models are intended to capture the behavior of systems in which individual social units (persons, organizations, animals, etc.) direct discrete actions towards other individuals in their environment. Within the `relevent` package, the `rem.dyad` function is the primary workhorse for modeling dyadic data. Although less flexible than `rem` (another `relevent` tool, not covered in this tutorial), `rem.dyad` contains many features that make it easier to work with in the dyadic case.

Data for use with `rem.dyad` consists of dynamic edge lists, each edge being characterized by a sender, a recipient, and an event time. (Currently, self-edges and undirected edges are not supported – this will change in future versions!) Ideally, event times are known exactly; however, under the piecewise constant hazard assumption (per Butts, 2008) the relational event family can still be identified up to a pacing constant so long as the order of events is known. Since the case of ordinal timing is somewhat simpler than that of exact timing, we consider it first.

```r
library(relevent)  #Load the relevent library
load("relevent_workshop.RData")  #Load the workshop data - may need to change directory!
```

1.1 Getting a look at the WTC Police radio data

The data we will use here comes from the World Trade Center radio communication data set coded by Butts et al. (2007). It consists of radio calls among 37 named communicants belonging to a police unit at the World Trade Center complex on the morning of 9/11/2001. The edgelist is contained in an object called `WTCPoliceCalls`; printing it should yield output like the following:

```r
WTCPoliceCalls
```

```
    number source recipient
1        1     16        32
2        2     32        16
3        3     16        32
4        4     16        32
5        5     11        32
6        6     11        32
7        7     11        32
8        8     36        32
9        9      8        32
10      10      8        32
11      11     32         8
12      12     16        32
13      13      8        32
14      14     26        32
15      15     32        26
```

16	16	26	32
17	17	32	26
18	18	26	32
19	19	32	26
20	20	16	32
21	21	16	32
22	22	27	32
23	23	20	32
24	24	32	20
25	25	20	32
26	26	32	20
27	27	32	16
28	28	16	32
29	29	32	16
30	30	32	16
31	31	16	32
32	32	32	22
33	33	3	32
34	34	32	3
35	35	3	32
36	36	32	3
37	37	32	16
38	38	16	32
39	39	32	16
40	40	3	32
41	41	3	32
42	42	32	3
43	43	3	32
44	44	16	3
45	45	16	11
46	46	11	16
47	47	16	11
48	48	11	16
49	49	16	11
50	50	11	16
51	51	24	36
52	52	24	36
53	53	15	32
54	54	32	15
55	55	15	32
56	56	32	15
57	57	15	32
58	58	32	15
59	59	22	32
60	60	32	22
61	61	15	32
62	62	32	15
63	63	15	32
64	64	32	15
65	65	18	32
66	66	32	18
67	67	18	32
68	68	19	32
69	69	32	19

70	70	19	32
71	71	32	19
72	72	19	32
73	73	16	32
74	74	32	16
75	75	16	32
76	76	32	16
77	77	36	16
78	78	16	36
79	79	36	16
80	80	16	36
81	81	36	16
82	82	16	36
83	83	27	32
84	84	32	16
85	85	16	32
86	86	32	16
87	87	16	32
88	88	32	16
89	89	22	15
90	90	15	22
91	91	22	15
92	92	15	22
93	93	22	15
94	94	16	22
95	95	22	16
96	96	16	22
97	97	22	11
98	98	11	22
99	99	36	32
100	100	32	36
101	101	36	32
102	102	32	36
103	103	36	32
104	104	32	36
105	105	27	32
106	106	37	32
107	107	32	37
108	108	37	32
109	109	32	37
110	110	5	32
111	111	32	5
112	112	5	32
113	113	32	5
114	114	31	36
115	115	36	31
116	116	31	36
117	117	36	31
118	118	37	32
119	119	16	32
120	120	32	16
121	121	16	32
122	122	32	16
123	123	29	32

124	124	32	29
125	125	37	14
126	126	29	32
127	127	31	32
128	128	32	37
129	129	16	32
130	130	32	16
131	131	16	32
132	132	32	16
133	133	16	32
134	134	36	16
135	135	16	36
136	136	36	16
137	137	16	36
138	138	29	32
139	139	8	35
140	140	32	16
141	141	8	35
142	142	32	16
143	143	16	32
144	144	32	16
145	145	16	32
146	146	22	32
147	147	32	22
148	148	22	32
149	149	32	22
150	150	27	32
151	151	32	27
152	152	27	32
153	153	32	26
154	154	22	32
155	155	32	22
156	156	22	32
157	157	32	22
158	158	22	32
159	159	32	22
160	160	22	32
161	161	32	22
162	162	16	32
163	163	32	16
164	164	16	32
165	165	32	16
166	166	16	32
167	167	16	11
168	168	27	32
169	169	32	16
170	170	16	32
171	171	32	16
172	172	36	32
173	173	32	36
174	174	36	32
175	175	32	36
176	176	16	32
177	177	32	16

178	178	16	32
179	179	32	16
180	180	16	32
181	181	32	16
182	182	16	32
183	183	10	2
184	184	2	10
185	185	10	26
186	186	16	32
187	187	32	16
188	188	16	32
189	189	16	32
190	190	32	16
191	191	32	16
192	192	16	32
193	193	32	16
194	194	16	32
195	195	32	16
196	196	16	32
197	197	32	16
198	198	16	32
199	199	32	16
200	200	16	32
201	201	32	16
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203	203	32	22
204	204	24	32
205	205	32	24
206	206	24	32
207	207	32	24
208	208	16	32
209	209	32	16
210	210	16	32
211	211	32	24
212	212	24	32
213	213	16	32
214	214	30	16
215	215	16	30
216	216	30	16
217	217	16	30
218	218	30	16
219	219	16	30
220	220	32	15
221	221	15	32
222	222	32	15
223	223	15	32
224	224	32	15
225	225	32	15
226	226	15	32
227	227	32	15
228	228	15	32
229	229	32	23
230	230	23	32
231	231	32	23

232	232	23	32
233	233	32	23
234	234	23	32
235	235	32	23
236	236	23	32
237	237	32	23
238	238	23	32
239	239	32	19
240	240	19	32
241	241	32	19
242	242	19	32
243	243	32	18
244	244	15	16
245	245	32	18
246	246	16	32
247	247	32	16
248	248	16	32
249	249	32	16
250	250	15	16
251	251	16	15
252	252	15	16
253	253	16	15
254	254	15	16
255	255	16	15
256	256	25	32
257	257	32	25
258	258	25	32
259	259	32	25
260	260	1	4
261	261	4	1
262	262	1	4
263	263	4	1
264	264	1	4
265	265	4	1
266	266	1	4
267	267	4	1
268	268	1	4
269	269	16	32
270	270	32	16
271	271	16	32
272	272	32	16
273	273	16	32
274	274	32	16
275	275	16	32
276	276	18	32
277	277	32	18
278	278	18	32
279	279	32	18
280	280	18	32
281	281	32	18
282	282	18	32
283	283	32	18
284	284	18	32
285	285	32	18

286	286	18	32
287	287	32	18
288	288	18	32
289	289	25	32
290	290	32	16
291	291	16	32
292	292	32	16
293	293	16	32
294	294	32	16
295	295	16	32
296	296	32	16
297	297	16	32
298	298	32	16
299	299	16	32
300	300	32	16
301	301	16	32
302	302	32	16
303	303	22	32
304	304	32	22
305	305	22	32
306	306	25	32
307	307	32	25
308	308	25	32
309	309	22	32
310	310	32	22
311	311	22	32
312	312	32	16
313	313	25	32
314	314	32	25
315	315	25	32
316	316	32	25
317	317	21	32
318	318	32	21
319	319	21	32
320	320	32	21
321	321	21	32
322	322	32	21
323	323	21	32
324	324	25	32
325	325	32	25
326	326	16	36
327	327	36	16
328	328	36	16
329	329	16	36
330	330	36	16
331	331	16	36
332	332	32	16
333	333	16	32
334	334	31	32
335	335	32	31
336	336	31	32
337	337	32	31
338	338	31	32
339	339	32	31

340	340	32	16
341	341	16	32
342	342	32	16
343	343	16	32
344	344	30	32
345	345	32	30
346	346	30	32
347	347	9	32
348	348	6	32
349	349	22	32
350	350	32	22
351	351	22	32
352	352	32	22
353	353	34	32
354	354	32	34
355	355	34	32
356	356	32	34
357	357	32	22
358	358	22	32
359	359	21	36
360	360	16	21
361	361	16	32
362	362	32	16
363	363	16	32
364	364	32	16
365	365	16	32
366	366	32	22
367	367	22	32
368	368	32	22
369	369	22	32
370	370	33	32
371	371	33	32
372	372	32	16
373	373	32	33
374	374	16	32
375	375	32	16
376	376	16	32
377	377	32	33
378	378	33	32
379	379	16	15
380	380	15	16
381	381	16	15
382	382	15	16
383	383	32	16
384	384	16	32
385	385	17	32
386	386	32	17
387	387	16	17
388	388	21	36
389	389	36	21
390	390	21	36
391	391	36	21
392	392	21	36
393	393	36	21

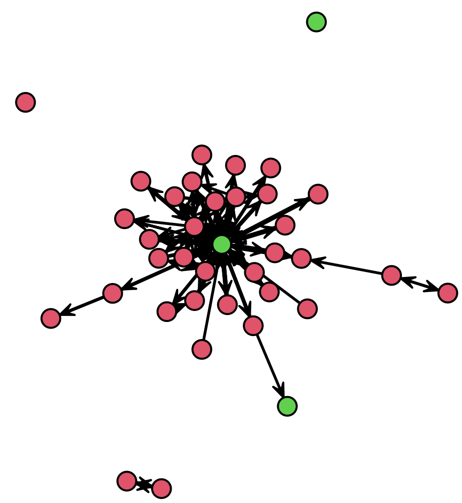
394	394	21	36
395	395	32	16
396	396	16	32
397	397	32	16
398	398	16	32
399	399	16	32
400	400	32	16
401	401	32	16
402	402	16	32
403	403	32	16
404	404	16	32
405	405	32	16
406	406	24	16
407	407	16	24
408	408	24	16
409	409	16	24
410	410	25	32
411	411	32	16
412	412	16	32
413	413	32	16
414	414	16	32
415	415	32	16
416	416	21	32
417	417	32	21
418	418	21	32
419	419	21	30
420	420	32	16
421	421	16	32
422	422	32	16
423	423	16	32
424	424	32	21
425	425	21	32
426	426	32	21
427	427	21	36
428	428	36	21
429	429	21	36
430	430	36	21
431	431	21	36
432	432	36	21
433	433	21	36
434	434	30	32
435	435	32	30
436	436	30	32
437	437	32	30
438	438	30	32
439	439	16	32
440	440	32	16
441	441	16	32
442	442	32	16
443	443	24	16
444	444	16	24
445	445	24	16
446	446	16	24
447	447	24	16

```
448    448     16          24
449    449     34          32
450    450     32          34
451    451     34          32
452    452     12          34
453    453     16          15
454    454     16          32
455    455     12          32
456    456     32          12
457    457     12          32
458    458     32          12
459    459     32          34
460    460     34          32
461    461     29          32
462    462     32          29
463    463     29          32
464    464     32          29
465    465     29          32
466    466     32          29
467    467     32          16
468    468     16          32
469    469     32          16
470    470     16          32
471    471     32          16
472    472     16          32
473    473     28          16
474    474     16          28
475    475     28          16
476    476     28          16
477    477     16          28
478    478     28          16
479    479     15          16
480    480     32          16
481    481     16          32
```

Note the form of the data: a matrix with the timing information, source (numbered from 1 to 37), and recipient (again numbered from 1 to 37) for each event (i.e., radio call). It is important to note that the WTC radio data was coded from transcripts that lacked detailed timing information; we do not therefore know precisely when these calls were made. We do, however, know the order in which calls were made, and can use this to fit relational event models with `rem.dyad`.

Before analyzing the data, it is helpful to consider what it looks like in time aggregated form. The helper function `as.sociomatrix.eventlist` is useful for this purpose: it converts an event list into a valued sociomatrix, of the form used by other `statnet` routines. Let's convert the data to sociomatrix form, and visualize it using the `gplot` function of the `sna` package:

```
WTCPoliceNet <- as.sociomatrix.eventlist(WTCPoliceCalls, 37)
gplot(WTCPoliceNet, edge.lwd = WTCPoliceNet^0.75, vertex.col = 2 +
   WTCPoliceIsICR, vertex.cex = 1.25)
```



In this visualization, we have scaled edge widths by communication volume – clearly, some pairs interact much more than others. Note also that we have colored vertices based on whether or not they occupy an institutionalized coordinative role (ICR), as indicated by the vector `WTCPoliceIsICR`. Those for whom this vector is TRUE (green) occupy roles within the police organization that would be expected to participate in coordinative activities; other actors were not identified as occupying such roles, based on the transcript data. In the analyses below, we will employ this covariate (as well as various endogenous mechanisms) to model the dynamics of radio communication within the WTC police network.

1.2 A first model: exploring ICR effects

Let's begin by fitting a very simple covariate model, in which the propensity of individuals to send and receive calls depends on whether they occupy institutionalized coordinative roles:

```
# First ICR effect - total interaction
wtcfit1 <- rem.dyad(WTCPoliceCalls, n = 37, effects = c("CovInt"),
   covar = list(CovInt = WTCPoliceIsICR), hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```
summary(wtcfit1)
```

```
Relational Event Model (Ordinal Likelihood)

         Estimate  Std.Err Z value  Pr(>|z|)
```

```
CovInt.1 2.104464 0.069817  30.142 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 6921.048 on 481 degrees of freedom
Residual deviance: 6193.998 on 480 degrees of freedom
    Chi-square: 727.0499 on 1 degrees of freedom, asymptotic p-value 0
AIC: 6195.998 AICC: 6196.007 BIC: 6200.174
```

The output gives us the covariate effect, as well as some uncertainty and goodness-of-fit information. The format is much like the output for a regression model, but coefficients should be interpreted per the relational event framework. In particular, the ICR role coefficient is the logged multiplier for the hazard of an event involving an ICR, versus a non-ICR event. (The effect is cumulative: an event in which one actor in an ICR calls another actor in an ICR gets twice the log increment.) We can see this impact in real terms as follows:

```
exp(wtcfit1$coef)  #Relative hazard for a non-ICR/ICR vs. a non-ICR/non-ICR event
```

```
CovInt.1
8.202708
```

```
exp(2 * wtcfit1$coef)  #Relative hazard for an ICR/ICR vs. a non-ICR/non-ICR event
```

```
CovInt.1
67.28442
```

We have here considered a homogeneous effect of ICR status on sending and receiving; is it worth treating these effects separately? To do so, we enter the ICR covariate as a sender and receiver covariate (respectively):

```
wtcfit2 <- rem.dyad(WTCPoliceCalls, n = 37, effects = c("CovSnd",
   "CovRec"), covar = list(CovSnd = WTCPoliceIsICR, CovRec = WTCPoliceIsICR),
   hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```
summary(wtcfit2)
```

```
Relational Event Model (Ordinal Likelihood)

         Estimate  Std.Err Z value  Pr(>|z|)
CovSnd.1 1.978870 0.095749  20.667 < 2.2e-16 ***
CovRec.1 2.225481 0.092863  23.965 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 6921.048 on 481 degrees of freedom
Residual deviance: 6190.175 on 479 degrees of freedom
    Chi-square: 730.8731 on 2 degrees of freedom, asymptotic p-value 0
AIC: 6194.175 AICC: 6194.2 BIC: 6202.527
```

Does the effect seem to differ? Let's see if fit improves (using the BIC):

```
wtcfit1$BIC - wtcfit2$BIC  #Model 1 a bit lower - we prefer it
```

```
[1] -2.352667
```

Model selection criteria are the preferred way to compare models, but one can also use a test of equality on the coefficients:

```
wtcfit2$coef  #Extract the coefficients
```

```
CovSnd.1 CovRec.1
1.978870 2.225481
```

```
wtcfit2$cov  #Likewise, the posterior covariance matrix
```

```
            [,1]        [,2]
[1,] 0.009167822 0.000900531
[2,] 0.000900531 0.008623620
```

```
# Heuristic Wald test of equality (not Bayesian, but
# whatever)
z <- diff(wtcfit2$coef)/sqrt(sum(diag(wtcfit2$cov)) - 2 * wtcfit2$cov[1,
   2])
z
```

```
CovRec.1
1.950214
```

```
2 * (1 - pnorm(abs(z)))  #Not conventionally significant - not strongly detectable
```

```
  CovRec.1
0.05115058
```

There might be some difference between the ICR sender and receiver effects, but it doesn't seem large enough to worry about. For now, we'll just stick with the simpler model (with a uniform effect on total interaction).

1.3 Bringing in endogenous social dynamics

One of the attractions of the relational event framework is its ability to capture endogenous social dynamics. In the following examples, we will examine several kinds of mechanisms that could conceivably impact communication among participants in the WTC police network. In each case, we first fit a candidate model, then compare that model to our best fitting model thus far identified. Where effects result in an improvement (as judged by the BIC), we include them in subsequent models.

To begin, we note that this is radio communication data. Radio communication is governed by strong conversational norms (in particular, radio SOP), which among other things mandate systematic turn-taking reciprocity. We can test for this via the use of participation shifts, particularly the AB-BA shift (a tendency for B to call A, given that A has just called B).

```
wtcfit3 <- rem.dyad(WTCPoliceCalls, n = 37, effects = c("CovInt",
   "PSAB-BA"), covar = list(CovInt = WTCPoliceIsICR), hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```
summary(wtcfit3)  #Looks like a strong effect...
```

```
Relational Event Model (Ordinal Likelihood)

         Estimate Std.Err Z value  Pr(>|z|)
CovInt.1  1.60405 0.11500  13.949 < 2.2e-16 ***
PSAB-BA   7.32695 0.10552  69.436 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Null deviance: 6921.048 on 481 degrees of freedom
Residual deviance: 2619.115 on 479 degrees of freedom
    Chi-square: 4301.933 on 2 degrees of freedom, asymptotic p-value 0
AIC: 2623.115 AICC: 2623.14 BIC: 2631.467
```

```
wtcfit1$BIC - wtcfit3$BIC  #We prefer model 3 to model 1 - reciprocity is in!
```

```
[1] 3568.707
```

```
exp(wtcfit3$coef["PSAB-BA"])  #Reciprocating events are >1500 times as likely
```

```
PSAB-BA
1520.73
```

What about other conversational norms? In general, we may expect that the current participants in an interaction may be likely to initiate the next call, a tendency that can also be captured with P-shift effects.

```
wtcfit4 <- rem.dyad(WTCPoliceCalls, n = 37, effects = c("CovInt",
   "PSAB-BA", "PSAB-BY", "PSAB-AY"), covar = list(CovInt = WTCPoliceIsICR),
   hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
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```

```
summary(wtcfit4)  #Seems like the effects are present, but let's test GOF...
```

```
Relational Event Model (Ordinal Likelihood)

         Estimate Std.Err Z value  Pr(>|z|)
CovInt.1  1.54282 0.11818 13.0548 < 2.2e-16 ***
PSAB-BA   7.49956 0.11418 65.6830 < 2.2e-16 ***
PSAB-BY   1.25942 0.25131  5.0115 5.401e-07 ***
PSAB-AY   0.87218 0.30611  2.8492  0.004383 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 6921.048 on 481 degrees of freedom
Residual deviance: 2595.135 on 477 degrees of freedom
    Chi-square: 4325.913 on 4 degrees of freedom, asymptotic p-value 0
AIC: 2603.135 AICC: 2603.219 BIC: 2619.839
```

```
wtcfit3$BIC - wtcfit4$BIC  #Yes, definite improvement
```

```
[1] 11.62806
```

P-shift effects are "local," in that they depend only on the prior event. What about effects of recency (from the point of view of ego) on the tendency to send calls to others?

```
wtcfit5 <- rem.dyad(WTCPoliceCalls, n = 37, effects = c("CovInt",
   "PSAB-BA", "PSAB-BY", "PSAB-AY", "RRecSnd", "RSndSnd"), covar = list(CovInt = WTCPoliceIsICR),
   hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
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```

```r
summary(wtcfit5)  #Looks good; note that AB-BA is much smaller than before
```

```
Relational Event Model (Ordinal Likelihood)

         Estimate Std.Err Z value  Pr(>|z|)
RRecSnd   2.38495 0.27447  8.6892 < 2.2e-16 ***
RSndSnd   1.34623 0.22307  6.0350 1.590e-09 ***
CovInt.1  1.07058 0.14244  7.5160 5.640e-14 ***
PSAB-BA   4.88714 0.15293 31.9569 < 2.2e-16 ***
PSAB-BY   1.67939 0.26116  6.4304 1.273e-10 ***
PSAB-AY   1.39017 0.31057  4.4762 7.597e-06 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 6921.048 on 481 degrees of freedom
Residual deviance: 2307.413 on 475 degrees of freedom
    Chi-square: 4613.635 on 6 degrees of freedom, asymptotic p-value 0
AIC: 2319.413 AICC: 2319.591 BIC: 2344.469
```

```r
wtcfit4$BIC - wtcfit5$BIC  #Substantial improvement
```

```
[1] 275.3701
```

Finally, recall what our relational event data looked like when viewed in time-aggregated form. We observed a strongly hub-dominated network, with a few actors doing most of the communication. Could this be explained in part via a preferential attachment mechanism (per de Sola Price and others), in which those having the most air time become the most attractive targets for others to call? We can investigate this by including normalized total degree as a predictor of tendency to receive calls:

```r
set.seed(13)  #To allow later results to be reproduced...
wtcfit6 <- rem.dyad(WTCPoliceCalls, n = 37, effects = c("CovInt",
   "PSAB-BA", "PSAB-BY", "PSAB-AY", "RRecSnd", "RSndSnd", "NTDegRec"),
   covar = list(CovInt = WTCPoliceIsICR), hessian = TRUE)
```

```
Prepping edgelist.
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```

```r
summary(wtcfit6)  #PA is drawing from recency, ICR effect, but not P-shifts
```

```
Relational Event Model (Ordinal Likelihood)

         Estimate Std.Err Z value  Pr(>|z|)
NTDegRec  3.13454 0.56678  5.5305 3.194e-08 ***
RRecSnd   2.02903 0.28500  7.1194 1.084e-12 ***
RSndSnd   0.87115 0.23846  3.6533 0.0002589 ***
CovInt.1  0.70734 0.16400  4.3129 1.611e-05 ***
PSAB-BA   5.32576 0.18236 29.2042 < 2.2e-16 ***
PSAB-BY   1.86023 0.26322  7.0674 1.579e-12 ***
PSAB-AY   1.64806 0.31092  5.3005 1.155e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 6921.048 on 481 degrees of freedom
Residual deviance: 2276.263 on 474 degrees of freedom
    Chi-square: 4644.785 on 7 degrees of freedom, asymptotic p-value 0
```

```
AIC: 2290.263 AICC: 2290.5 BIC: 2319.494
```

```r
wtcfit5$BIC - wtcfit6$BIC  #Model is preferred
```

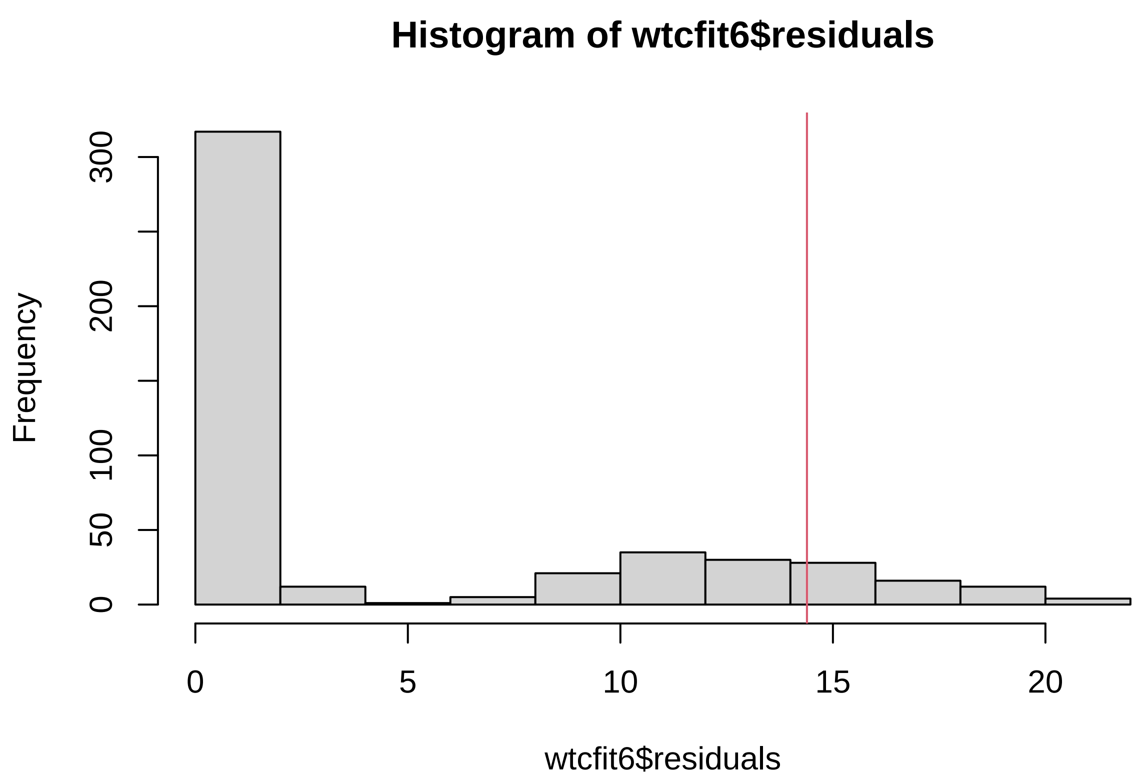
```
[1] 24.97434
```

At this point, we've got a decent quorum of effects, and the deviance reduction is substantial. Of course, we could continue to investigate other mechanisms; see `?rem.dyad` for the full range of options.

1.4 Assessing model adequacy

Model adequacy is an important consideration: even given that our model is the best of those we've seen, is it good enough for our purposes? There are many ways to assess model adequacy; here, we focus on the ability of the relational event model to predict the next event in the sequence, given those that have come before. A natural question to ask when assessing the model is to ask when it is "surprised:" when does it encounter observations that are relatively poorly predicted? To investigate this, we can examine the deviance residuals:

```r
nullresid <- 2 * log(37 * 36)  #What would be the deviance residual for the null?
hist(wtcfit6$residuals)  #Deviance residuals - most well-predicted, some around chance levels
abline(v = nullresid, col = 2)
```




```r
mean(wtcfit6$residuals < nullresid)  #Beating chance on almost all...
```

```
[1] 0.8898129
```

```r
mean(wtcfit6$residuals < 3)  #Upper limit of lower cluster is about 3
```

```
[1] 0.6839917
```

We seem to be doing pretty well here. As another way of evaluating the deviance residuals for the ordinal model, it is useful to note that the quantity $\exp(DR/2)$ (where DR is the deviance residual) is a "random guessing equivalent," or an effective number of events such that a random guess among such events as to which is coming next would be right as often as the model expects to be. We can easily compute this as follows:

```
quantile(exp(wtcfit6$residuals/2))  #'Random guessing equivalent' (ref is 1332)
```

```
         0%          25%          50%          75%         100%
   1.073634     1.268661     1.739723   204.538728 31633.030288
```

Note that there are 1332 possible events, so we are doing much, much better than an uninformative baseline. Likewise, we've come a long way from our initial model:

```
quantile(exp(wtcfit1$residuals/2))  #By comparison, first model much worse!
```

```
       0%       25%       50%       75%      100%
 390.0003  390.0003  390.0003  390.0003 3199.0589
```

In addition to overall examination of residuals, it can be useful to ask which particular events seem to be sources of surprise:

```
cbind(WTCPoliceCalls, wtcfit6$residuals > nullresid)  #Which are the more surprising cases?
```

```
   number source recipient wtcfit6$residuals > nullresid
1       1     16        32                         FALSE
2       2     32        16                         FALSE
3       3     16        32                         FALSE
4       4     16        32                         FALSE
5       5     11        32                          TRUE
6       6     11        32                         FALSE
7       7     11        32                         FALSE
8       8     36        32                         FALSE
9       9      8        32                         FALSE
10     10      8        32                         FALSE
11     11     32         8                         FALSE
12     12     16        32                         FALSE
13     13      8        32                         FALSE
14     14     26        32                          TRUE
15     15     32        26                         FALSE
16     16     26        32                         FALSE
17     17     32        26                         FALSE
18     18     26        32                         FALSE
19     19     32        26                         FALSE
20     20     16        32                         FALSE
21     21     16        32                         FALSE
22     22     27        32                         FALSE
23     23     20        32                         FALSE
24     24     32        20                         FALSE
25     25     20        32                         FALSE
26     26     32        20                         FALSE
27     27     32        16                         FALSE
28     28     16        32                         FALSE
29     29     32        16                         FALSE
30     30     32        16                         FALSE
31     31     16        32                         FALSE
32     32     32        22                         FALSE
33     33      3        32                          TRUE
```

34	34	32	3	FALSE
35	35	3	32	FALSE
36	36	32	3	FALSE
37	37	32	16	FALSE
38	38	16	32	FALSE
39	39	32	16	FALSE
40	40	3	32	FALSE
41	41	3	32	FALSE
42	42	32	3	FALSE
43	43	3	32	FALSE
44	44	16	3	TRUE
45	45	16	11	FALSE
46	46	11	16	FALSE
47	47	16	11	FALSE
48	48	11	16	FALSE
49	49	16	11	FALSE
50	50	11	16	FALSE
51	51	24	36	TRUE
52	52	24	36	TRUE
53	53	15	32	FALSE
54	54	32	15	FALSE
55	55	15	32	FALSE
56	56	32	15	FALSE
57	57	15	32	FALSE
58	58	32	15	FALSE
59	59	22	32	FALSE
60	60	32	22	FALSE
61	61	15	32	FALSE
62	62	32	15	FALSE
63	63	15	32	FALSE
64	64	32	15	FALSE
65	65	18	32	TRUE
66	66	32	18	FALSE
67	67	18	32	FALSE
68	68	19	32	TRUE
69	69	32	19	FALSE
70	70	19	32	FALSE
71	71	32	19	FALSE
72	72	19	32	FALSE
73	73	16	32	FALSE
74	74	32	16	FALSE
75	75	16	32	FALSE
76	76	32	16	FALSE
77	77	36	16	TRUE
78	78	16	36	FALSE
79	79	36	16	FALSE
80	80	16	36	FALSE
81	81	36	16	FALSE
82	82	16	36	FALSE
83	83	27	32	FALSE
84	84	32	16	FALSE
85	85	16	32	FALSE
86	86	32	16	FALSE
87	87	16	32	FALSE

88	88	32	16	FALSE
89	89	22	15	TRUE
90	90	15	22	FALSE
91	91	22	15	FALSE
92	92	15	22	FALSE
93	93	22	15	FALSE
94	94	16	22	TRUE
95	95	22	16	FALSE
96	96	16	22	FALSE
97	97	22	11	TRUE
98	98	11	22	FALSE
99	99	36	32	FALSE
100	100	32	36	FALSE
101	101	36	32	FALSE
102	102	32	36	FALSE
103	103	36	32	FALSE
104	104	32	36	FALSE
105	105	27	32	TRUE
106	106	37	32	FALSE
107	107	32	37	FALSE
108	108	37	32	FALSE
109	109	32	37	FALSE
110	110	5	32	TRUE
111	111	32	5	FALSE
112	112	5	32	FALSE
113	113	32	5	FALSE
114	114	31	36	TRUE
115	115	36	31	FALSE
116	116	31	36	FALSE
117	117	36	31	FALSE
118	118	37	32	FALSE
119	119	16	32	FALSE
120	120	32	16	FALSE
121	121	16	32	FALSE
122	122	32	16	FALSE
123	123	29	32	TRUE
124	124	32	29	FALSE
125	125	37	14	TRUE
126	126	29	32	FALSE
127	127	31	32	TRUE
128	128	32	37	FALSE
129	129	16	32	FALSE
130	130	32	16	FALSE
131	131	16	32	FALSE
132	132	32	16	FALSE
133	133	16	32	FALSE
134	134	36	16	TRUE
135	135	16	36	FALSE
136	136	36	16	FALSE
137	137	16	36	FALSE
138	138	29	32	FALSE
139	139	8	35	TRUE
140	140	32	16	FALSE
141	141	8	35	TRUE

142	142	32	16	FALSE
143	143	16	32	FALSE
144	144	32	16	FALSE
145	145	16	32	FALSE
146	146	22	32	FALSE
147	147	32	22	FALSE
148	148	22	32	FALSE
149	149	32	22	FALSE
150	150	27	32	TRUE
151	151	32	27	FALSE
152	152	27	32	FALSE
153	153	32	26	FALSE
154	154	22	32	FALSE
155	155	32	22	FALSE
156	156	22	32	FALSE
157	157	32	22	FALSE
158	158	22	32	FALSE
159	159	32	22	FALSE
160	160	22	32	FALSE
161	161	32	22	FALSE
162	162	16	32	FALSE
163	163	32	16	FALSE
164	164	16	32	FALSE
165	165	32	16	FALSE
166	166	16	32	FALSE
167	167	16	11	TRUE
168	168	27	32	FALSE
169	169	32	16	FALSE
170	170	16	32	FALSE
171	171	32	16	FALSE
172	172	36	32	TRUE
173	173	32	36	FALSE
174	174	36	32	FALSE
175	175	32	36	FALSE
176	176	16	32	FALSE
177	177	32	16	FALSE
178	178	16	32	FALSE
179	179	32	16	FALSE
180	180	16	32	FALSE
181	181	32	16	FALSE
182	182	16	32	FALSE
183	183	10	2	TRUE
184	184	2	10	FALSE
185	185	10	26	FALSE
186	186	16	32	FALSE
187	187	32	16	FALSE
188	188	16	32	FALSE
189	189	16	32	FALSE
190	190	32	16	FALSE
191	191	32	16	FALSE
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194	194	16	32	FALSE
195	195	32	16	FALSE

196	196	16	32	FALSE
197	197	32	16	FALSE
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199	199	32	16	FALSE
200	200	16	32	FALSE
201	201	32	16	FALSE
202	202	22	32	FALSE
203	203	32	22	FALSE
204	204	24	32	TRUE
205	205	32	24	FALSE
206	206	24	32	FALSE
207	207	32	24	FALSE
208	208	16	32	FALSE
209	209	32	16	FALSE
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213	213	16	32	FALSE
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217	217	16	30	FALSE
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220	220	32	15	TRUE
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223	223	15	32	FALSE
224	224	32	15	FALSE
225	225	32	15	FALSE
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230	230	23	32	FALSE
231	231	32	23	FALSE
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235	235	32	23	FALSE
236	236	23	32	FALSE
237	237	32	23	FALSE
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240	240	19	32	FALSE
241	241	32	19	FALSE
242	242	19	32	FALSE
243	243	32	18	FALSE
244	244	15	16	TRUE
245	245	32	18	FALSE
246	246	16	32	TRUE
247	247	32	16	FALSE
248	248	16	32	FALSE
249	249	32	16	FALSE

250	250	15	16	TRUE
251	251	16	15	FALSE
252	252	15	16	FALSE
253	253	16	15	FALSE
254	254	15	16	FALSE
255	255	16	15	FALSE
256	256	25	32	TRUE
257	257	32	25	FALSE
258	258	25	32	FALSE
259	259	32	25	FALSE
260	260	1	4	TRUE
261	261	4	1	FALSE
262	262	1	4	FALSE
263	263	4	1	FALSE
264	264	1	4	FALSE
265	265	4	1	FALSE
266	266	1	4	FALSE
267	267	4	1	FALSE
268	268	1	4	FALSE
269	269	16	32	FALSE
270	270	32	16	FALSE
271	271	16	32	FALSE
272	272	32	16	FALSE
273	273	16	32	FALSE
274	274	32	16	FALSE
275	275	16	32	FALSE
276	276	18	32	FALSE
277	277	32	18	FALSE
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284	284	18	32	FALSE
285	285	32	18	FALSE
286	286	18	32	FALSE
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288	288	18	32	FALSE
289	289	25	32	FALSE
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293	293	16	32	FALSE
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296	296	32	16	FALSE
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300	300	32	16	FALSE
301	301	16	32	FALSE
302	302	32	16	FALSE
303	303	22	32	FALSE

304	304	32	22	FALSE
305	305	22	32	FALSE
306	306	25	32	FALSE
307	307	32	25	FALSE
308	308	25	32	FALSE
309	309	22	32	FALSE
310	310	32	22	FALSE
311	311	22	32	FALSE
312	312	32	16	FALSE
313	313	25	32	FALSE
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323	323	21	32	FALSE
324	324	25	32	FALSE
325	325	32	25	FALSE
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328	328	36	16	FALSE
329	329	16	36	FALSE
330	330	36	16	FALSE
331	331	16	36	FALSE
332	332	32	16	TRUE
333	333	16	32	FALSE
334	334	31	32	FALSE
335	335	32	31	FALSE
336	336	31	32	FALSE
337	337	32	31	FALSE
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339	339	32	31	FALSE
340	340	32	16	FALSE
341	341	16	32	FALSE
342	342	32	16	FALSE
343	343	16	32	FALSE
344	344	30	32	TRUE
345	345	32	30	FALSE
346	346	30	32	FALSE
347	347	9	32	TRUE
348	348	6	32	FALSE
349	349	22	32	FALSE
350	350	32	22	FALSE
351	351	22	32	FALSE
352	352	32	22	FALSE
353	353	34	32	TRUE
354	354	32	34	FALSE
355	355	34	32	FALSE
356	356	32	34	FALSE
357	357	32	22	FALSE

358	358	22	32	FALSE
359	359	21	36	TRUE
360	360	16	21	TRUE
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362	362	32	16	FALSE
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364	364	32	16	FALSE
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368	368	32	22	FALSE
369	369	22	32	FALSE
370	370	33	32	TRUE
371	371	33	32	FALSE
372	372	32	16	FALSE
373	373	32	33	FALSE
374	374	16	32	FALSE
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376	376	16	32	FALSE
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378	378	33	32	FALSE
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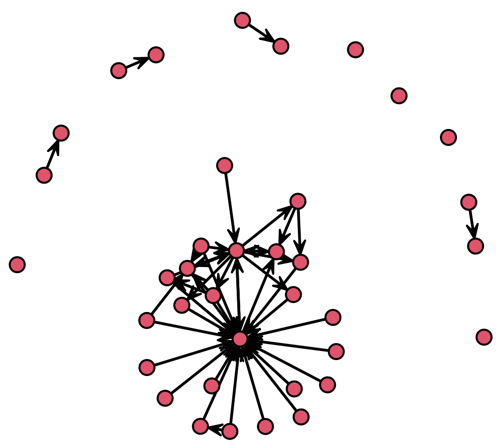
380	380	15	16	FALSE
381	381	16	15	FALSE
382	382	15	16	FALSE
383	383	32	16	FALSE
384	384	16	32	FALSE
385	385	17	32	TRUE
386	386	32	17	FALSE
387	387	16	17	TRUE
388	388	21	36	TRUE
389	389	36	21	FALSE
390	390	21	36	FALSE
391	391	36	21	FALSE
392	392	21	36	FALSE
393	393	36	21	FALSE
394	394	21	36	FALSE
395	395	32	16	FALSE
396	396	16	32	FALSE
397	397	32	16	FALSE
398	398	16	32	FALSE
399	399	16	32	FALSE
400	400	32	16	FALSE
401	401	32	16	FALSE
402	402	16	32	FALSE
403	403	32	16	FALSE
404	404	16	32	FALSE
405	405	32	16	FALSE
406	406	24	16	TRUE
407	407	16	24	FALSE
408	408	24	16	FALSE
409	409	16	24	FALSE
410	410	25	32	FALSE
411	411	32	16	FALSE

412	412	16	32	FALSE
413	413	32	16	FALSE
414	414	16	32	FALSE
415	415	32	16	FALSE
416	416	21	32	TRUE
417	417	32	21	FALSE
418	418	21	32	FALSE
419	419	21	30	TRUE
420	420	32	16	FALSE
421	421	16	32	FALSE
422	422	32	16	FALSE
423	423	16	32	FALSE
424	424	32	21	FALSE
425	425	21	32	FALSE
426	426	32	21	FALSE
427	427	21	36	FALSE
428	428	36	21	FALSE
429	429	21	36	FALSE
430	430	36	21	FALSE
431	431	21	36	FALSE
432	432	36	21	FALSE
433	433	21	36	FALSE
434	434	30	32	FALSE
435	435	32	30	FALSE
436	436	30	32	FALSE
437	437	32	30	FALSE
438	438	30	32	FALSE
439	439	16	32	FALSE
440	440	32	16	FALSE
441	441	16	32	FALSE
442	442	32	16	FALSE
443	443	24	16	FALSE
444	444	16	24	FALSE
445	445	24	16	FALSE
446	446	16	24	FALSE
447	447	24	16	FALSE
448	448	16	24	FALSE
449	449	34	32	FALSE
450	450	32	34	FALSE
451	451	34	32	FALSE
452	452	12	34	TRUE
453	453	16	15	TRUE
454	454	16	32	FALSE
455	455	12	32	TRUE
456	456	32	12	FALSE
457	457	12	32	FALSE
458	458	32	12	FALSE
459	459	32	34	FALSE
460	460	34	32	FALSE
461	461	29	32	FALSE
462	462	32	29	FALSE
463	463	29	32	FALSE
464	464	32	29	FALSE
465	465	29	32	FALSE

```
466    466     32         29                          FALSE
467    467     32         16                          FALSE
468    468     16         32                          FALSE
469    469     32         16                          FALSE
470    470     16         32                          FALSE
471    471     32         16                          FALSE
472    472     16         32                          FALSE
473    473     28         16                           TRUE
474    474     16         28                          FALSE
475    475     28         16                          FALSE
476    476     28         16                          FALSE
477    477     16         28                          FALSE
478    478     28         16                          FALSE
479    479     15         16                          FALSE
480    480     32         16                          FALSE
481    481     16         32                          FALSE
```

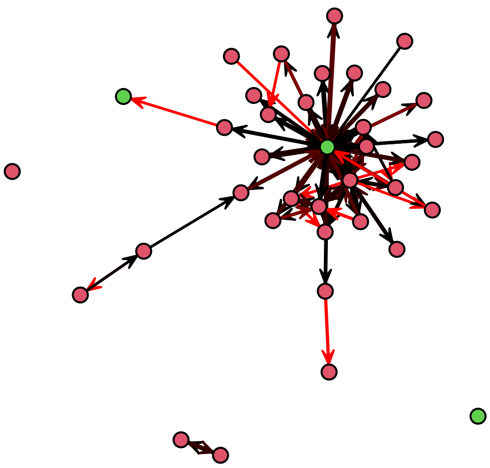
Using `as.sociomatrix.eventlist`, we can even pull out these events and view them in time-aggregated form. This can give us a better sense of the structural context in which they occur:

```
surprising <- as.sociomatrix.eventlist(WTCPoliceCalls[wtcfit6$residuals >
   nullresid, ], 37)
gplot(surprising)  #Plot in network form
```



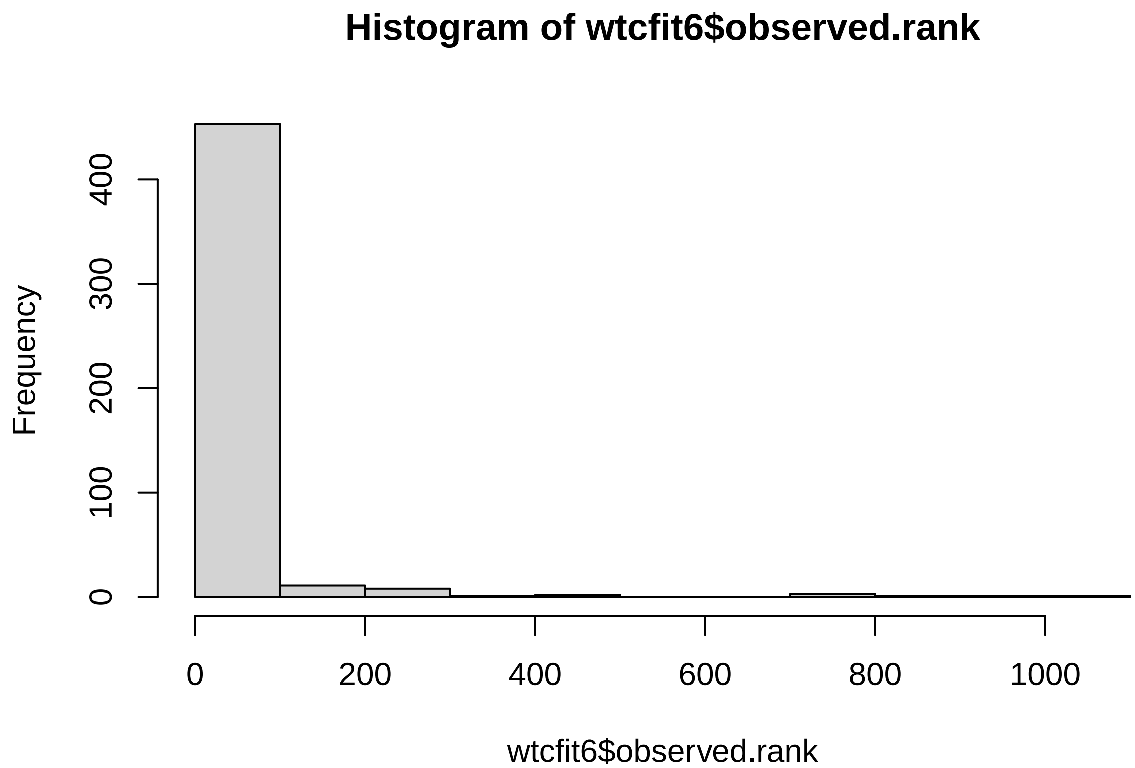
```
# Can also superimpose on the original network (coloring
# edges by fraction surprising)
edgecol <- matrix(rgb(surprising/(WTCPoliceNet + 0.01), 0, 0),
```

```
    37, 37)  #Color me surprised
gplot(WTCPoliceNet, edge.col = edgecol, edge.lwd = WTCPoliceNet^0.75,
    vertex.col = 2 + WTCPoliceIsICR)
```



Yet another approach to adequacy assessment is to consider the rank of the observed events in the predicted rate structure: that is, we ask to what extent the events viewed most likely to occur are in fact those that are observed.

```
hist(wtcfit6$observed.rank)
```




```
cbind(WTCPoliceCalls, wtcfit6$observed.rank)  #Histogram of ranks
```

```
   number source recipient wtcfit6$observed.rank
1       1     16        32                     7
2       2     32        16                     1
3       3     16        32                     1
4       4     16        32                     2
5       5     11        32                    42
6       6     11        32                     6
7       7     11        32                     6
8       8     36        32                    44
9       9      8        32                    45
10     10      8        32                     8
11     11     32         8                     1
12     12     16        32                     2
13     13      8        32                     2
14     14     26        32                    45
15     15     32        26                     1
16     16     26        32                     1
17     17     32        26                     1
18     18     26        32                     1
19     19     32        26                     1
20     20     16        32                     2
21     21     16        32                     2
22     22     27        32                    46
23     23     20        32                    47
```

24	24	32	20	1
25	25	20	32	1
26	26	32	20	1
27	27	32	16	6
28	28	16	32	1
29	29	32	16	1
30	30	32	16	5
31	31	16	32	1
32	32	32	22	19
33	33	3	32	49
34	34	32	3	1
35	35	3	32	1
36	36	32	3	1
37	37	32	16	7
38	38	16	32	1
39	39	32	16	1
40	40	3	32	2
41	41	3	32	2
42	42	32	3	1
43	43	3	32	1
44	44	16	3	276
45	45	16	11	79
46	46	11	16	1
47	47	16	11	1
48	48	11	16	1
49	49	16	11	1
50	50	11	16	1
51	51	24	36	465
52	52	24	36	128
53	53	15	32	28
54	54	32	15	1
55	55	15	32	1
56	56	32	15	1
57	57	15	32	1
58	58	32	15	1
59	59	22	32	5
60	60	32	22	1
61	61	15	32	2
62	62	32	15	1
63	63	15	32	1
64	64	32	15	1
65	65	18	32	58
66	66	32	18	1
67	67	18	32	1
68	68	19	32	57
69	69	32	19	1
70	70	19	32	1
71	71	32	19	1
72	72	19	32	1
73	73	16	32	13
74	74	32	16	1
75	75	16	32	1
76	76	32	16	1
77	77	36	16	248

78	78	16	36	1
79	79	36	16	1
80	80	16	36	1
81	81	36	16	1
82	82	16	36	1
83	83	27	32	16
84	84	32	16	2
85	85	16	32	1
86	86	32	16	1
87	87	16	32	1
88	88	32	16	1
89	89	22	15	279
90	90	15	22	1
91	91	22	15	1
92	92	15	22	1
93	93	22	15	1
94	94	16	22	434
95	95	22	16	1
96	96	16	22	1
97	97	22	11	29
98	98	11	22	1
99	99	36	32	28
100	100	32	36	1
101	101	36	32	1
102	102	32	36	1
103	103	36	32	1
104	104	32	36	1
105	105	27	32	25
106	106	37	32	62
107	107	32	37	1
108	108	37	32	1
109	109	32	37	1
110	110	5	32	72
111	111	32	5	1
112	112	5	32	1
113	113	32	5	1
114	114	31	36	286
115	115	36	31	1
116	116	31	36	1
117	117	36	31	1
118	118	37	32	3
119	119	16	32	13
120	120	32	16	1
121	121	16	32	1
122	122	32	16	1
123	123	29	32	75
124	124	32	29	1
125	125	37	14	158
126	126	29	32	3
127	127	31	32	66
128	128	32	37	15
129	129	16	32	2
130	130	32	16	1
131	131	16	32	1

132	132	32	16	1
133	133	16	32	1
134	134	36	16	118
135	135	16	36	1
136	136	36	16	1
137	137	16	36	1
138	138	29	32	3
139	139	8	35	789
140	140	32	16	15
141	141	8	35	128
142	142	32	16	15
143	143	16	32	1
144	144	32	16	1
145	145	16	32	1
146	146	22	32	42
147	147	32	22	1
148	148	22	32	1
149	149	32	22	1
150	150	27	32	30
151	151	32	27	1
152	152	27	32	1
153	153	32	26	32
154	154	22	32	3
155	155	32	22	1
156	156	22	32	1
157	157	32	22	1
158	158	22	32	1
159	159	32	22	1
160	160	22	32	1
161	161	32	22	1
162	162	16	32	2
163	163	32	16	1
164	164	16	32	1
165	165	32	16	1
166	166	16	32	1
167	167	16	11	62
168	168	27	32	3
169	169	32	16	2
170	170	16	32	1
171	171	32	16	1
172	172	36	32	28
173	173	32	36	1
174	174	36	32	1
175	175	32	36	1
176	176	16	32	2
177	177	32	16	1
178	178	16	32	1
179	179	32	16	1
180	180	16	32	1
181	181	32	16	1
182	182	16	32	1
183	183	10	2	821
184	184	2	10	1
185	185	10	26	60

186	186	16	32	3
187	187	32	16	1
188	188	16	32	1
189	189	16	32	2
190	190	32	16	1
191	191	32	16	12
192	192	16	32	1
193	193	32	16	1
194	194	16	32	1
195	195	32	16	1
196	196	16	32	1
197	197	32	16	1
198	198	16	32	1
199	199	32	16	1
200	200	16	32	1
201	201	32	16	1
202	202	22	32	2
203	203	32	22	1
204	204	24	32	72
205	205	32	24	1
206	206	24	32	1
207	207	32	24	1
208	208	16	32	2
209	209	32	16	1
210	210	16	32	1
211	211	32	24	14
212	212	24	32	1
213	213	16	32	2
214	214	30	16	260
215	215	16	30	1
216	216	30	16	1
217	217	16	30	1
218	218	30	16	1
219	219	16	30	1
220	220	32	15	136
221	221	15	32	1
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223	223	15	32	1
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225	225	32	15	16
226	226	15	32	1
227	227	32	15	1
228	228	15	32	1
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233	233	32	23	1
234	234	23	32	1
235	235	32	23	1
236	236	23	32	1
237	237	32	23	1
238	238	23	32	1
239	239	32	19	35

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241	241	32	19	1
242	242	19	32	1
243	243	32	18	37
244	244	15	16	265
245	245	32	18	91
246	246	16	32	22
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248	248	16	32	1
249	249	32	16	1
250	250	15	16	121
251	251	16	15	1
252	252	15	16	1
253	253	16	15	1
254	254	15	16	1
255	255	16	15	1
256	256	25	32	46
257	257	32	25	1
258	258	25	32	1
259	259	32	25	1
260	260	1	4	981
261	261	4	1	1
262	262	1	4	1
263	263	4	1	1
264	264	1	4	1
265	265	4	1	1
266	266	1	4	1
267	267	4	1	1
268	268	1	4	1
269	269	16	32	22
270	270	32	16	1
271	271	16	32	1
272	272	32	16	1
273	273	16	32	1
274	274	32	16	1
275	275	16	32	1
276	276	18	32	2
277	277	32	18	1
278	278	18	32	1
279	279	32	18	1
280	280	18	32	1
281	281	32	18	1
282	282	18	32	1
283	283	32	18	1
284	284	18	32	1
285	285	32	18	1
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287	287	32	18	1
288	288	18	32	1
289	289	25	32	2
290	290	32	16	17
291	291	16	32	1
292	292	32	16	1
293	293	16	32	1

294	294	32	16	1
295	295	16	32	1
296	296	32	16	1
297	297	16	32	1
298	298	32	16	1
299	299	16	32	1
300	300	32	16	1
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303	303	22	32	2
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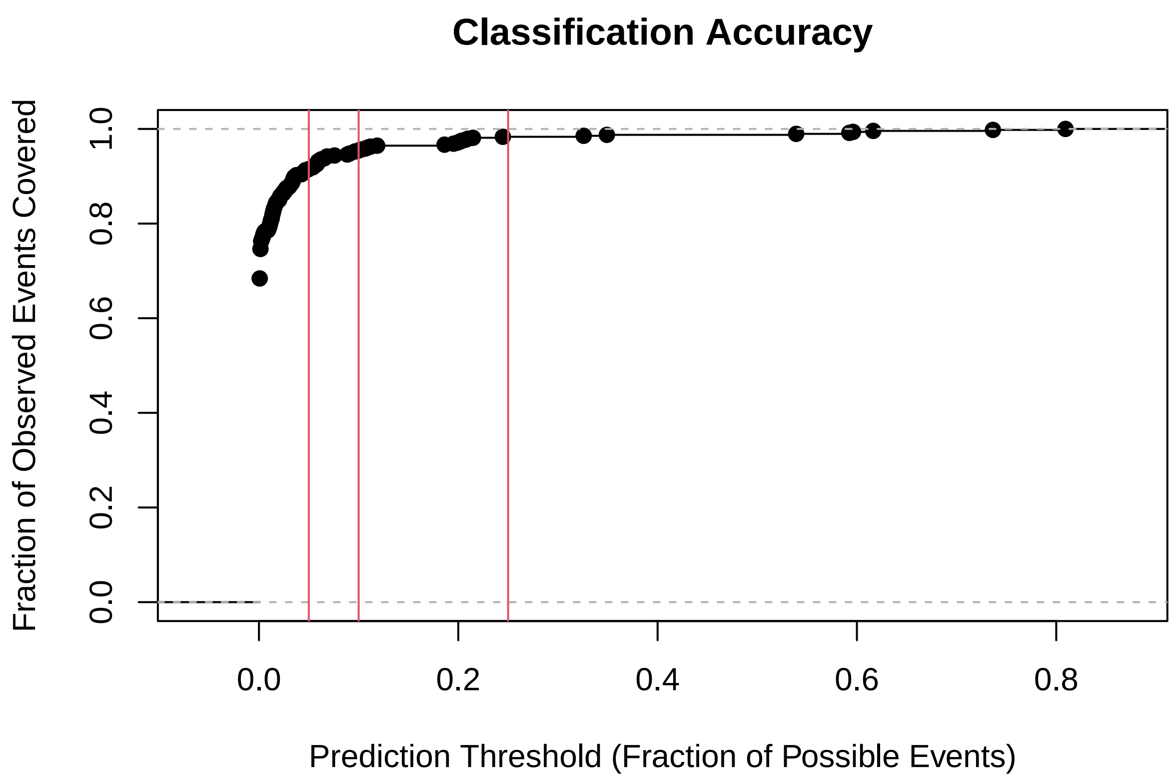
306	306	25	32	2
307	307	32	25	1
308	308	25	32	1
309	309	22	32	2
310	310	32	22	1
311	311	22	32	1
312	312	32	16	16
313	313	25	32	3
314	314	32	25	1
315	315	25	32	1
316	316	32	25	1
317	317	21	32	78
318	318	32	21	1
319	319	21	32	1
320	320	32	21	1
321	321	21	32	1
322	322	32	21	1
323	323	21	32	1
324	324	25	32	2
325	325	32	25	1
326	326	16	36	142
327	327	36	16	1
328	328	36	16	20
329	329	16	36	1
330	330	36	16	1
331	331	16	36	1
332	332	32	16	47
333	333	16	32	1
334	334	31	32	40
335	335	32	31	1
336	336	31	32	1
337	337	32	31	1
338	338	31	32	1
339	339	32	31	1
340	340	32	16	14
341	341	16	32	1
342	342	32	16	1
343	343	16	32	1
344	344	30	32	79
345	345	32	30	1
346	346	30	32	1
347	347	9	32	75

348	348	6	32	77
349	349	22	32	2
350	350	32	22	1
351	351	22	32	1
352	352	32	22	1
353	353	34	32	81
354	354	32	34	1
355	355	34	32	1
356	356	32	34	1
357	357	32	22	18
358	358	22	32	1
359	359	21	36	326
360	360	16	21	718
361	361	16	32	2
362	362	32	16	1
363	363	16	32	1
364	364	32	16	1
365	365	16	32	1
366	366	32	22	18
367	367	22	32	1
368	368	32	22	1
369	369	22	32	1
370	370	33	32	83
371	371	33	32	44
372	372	32	16	19
373	373	32	33	17
374	374	16	32	2
375	375	32	16	1
376	376	16	32	1
377	377	32	33	19
378	378	33	32	1
379	379	16	15	133
380	380	15	16	1
381	381	16	15	1
382	382	15	16	1
383	383	32	16	33
384	384	16	32	1
385	385	17	32	87
386	386	32	17	1
387	387	16	17	1078
388	388	21	36	145
389	389	36	21	1
390	390	21	36	1
391	391	36	21	1
392	392	21	36	1
393	393	36	21	1
394	394	21	36	1
395	395	32	16	36
396	396	16	32	1
397	397	32	16	1
398	398	16	32	1
399	399	16	32	2
400	400	32	16	1
401	401	32	16	18

402	402	16	32	1
403	403	32	16	1
404	404	16	32	1
405	405	32	16	1
406	406	24	16	268
407	407	16	24	1
408	408	24	16	1
409	409	16	24	1
410	410	25	32	4
411	411	32	16	2
412	412	16	32	1
413	413	32	16	1
414	414	16	32	1
415	415	32	16	1
416	416	21	32	33
417	417	32	21	1
418	418	21	32	1
419	419	21	30	101
420	420	32	16	36
421	421	16	32	1
422	422	32	16	1
423	423	16	32	1
424	424	32	21	18
425	425	21	32	1
426	426	32	21	1
427	427	21	36	27
428	428	36	21	1
429	429	21	36	1
430	430	36	21	1
431	431	21	36	1
432	432	36	21	1
433	433	21	36	1
434	434	30	32	20
435	435	32	30	1
436	436	30	32	1
437	437	32	30	1
438	438	30	32	1
439	439	16	32	2
440	440	32	16	1
441	441	16	32	1
442	442	32	16	1
443	443	24	16	22
444	444	16	24	1
445	445	24	16	1
446	446	16	24	1
447	447	24	16	1
448	448	16	24	1
449	449	34	32	4
450	450	32	34	1
451	451	34	32	1
452	452	12	34	794
453	453	16	15	149
454	454	16	32	3
455	455	12	32	91

456	456	32	12	1
457	457	12	32	1
458	458	32	12	1
459	459	32	34	25
460	460	34	32	1
461	461	29	32	2
462	462	32	29	1
463	463	29	32	1
464	464	32	29	1
465	465	29	32	1
466	466	32	29	1
467	467	32	16	22
468	468	16	32	1
469	469	32	16	1
470	470	16	32	1
471	471	32	16	1
472	472	16	32	1
473	473	28	16	271
474	474	16	28	1
475	475	28	16	1
476	476	28	16	23
477	477	16	28	1
478	478	28	16	1
479	479	15	16	23
480	480	32	16	20
481	481	16	32	1

```
# Rank on a per-event basis (low is good) Sometimes useful
# to plot the ECDF of the observed ranks....
plot(ecdf(wtcfit6$observed.rank/(37 * 36)), xlab = "Prediction Threshold (Fraction of Possible Events)"
   ylab = "Fraction of Observed Events Covered", main = "Classification Accuracy")
abline(v = c(0.05, 0.1, 0.25), col = 2)
```



As the above indicates, we sometimes (in fact often) manage to get things exactly right: that is, the event predicted most likely to be the next in the sequence is in fact the one that is observed. Examining the match rate is a very strict notion of adequacy, but can be useful for assessing models that are strongly predictive.

```
wtcfit6$predicted.match  #Exactly correct src/target
```

```
       source recipient
 [1,]  FALSE     FALSE
 [2,]   TRUE      TRUE
 [3,]   TRUE      TRUE
 [4,]  FALSE     FALSE
 [5,]  FALSE     FALSE
 [6,]  FALSE     FALSE
 [7,]  FALSE     FALSE
 [8,]  FALSE     FALSE
 [9,]  FALSE     FALSE
[10,]  FALSE     FALSE
[11,]   TRUE      TRUE
[12,]  FALSE      TRUE
[13,]  FALSE     FALSE
[14,]  FALSE     FALSE
[15,]   TRUE      TRUE
[16,]   TRUE      TRUE
[17,]   TRUE      TRUE
[18,]   TRUE      TRUE
[19,]   TRUE      TRUE
[20,]  FALSE      TRUE
```

```
[21,]  FALSE     FALSE
[22,]  FALSE     FALSE
[23,]  FALSE     FALSE
[24,]   TRUE      TRUE
[25,]   TRUE      TRUE
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[27,]  FALSE     FALSE
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[32,]   TRUE     FALSE
[33,]  FALSE      TRUE
[34,]   TRUE      TRUE
[35,]   TRUE      TRUE
[36,]   TRUE      TRUE
[37,]  FALSE     FALSE
[38,]   TRUE      TRUE
[39,]   TRUE      TRUE
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[41,]  FALSE     FALSE
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[68,]  FALSE     FALSE
[69,]   TRUE      TRUE
[70,]   TRUE      TRUE
[71,]   TRUE      TRUE
[72,]   TRUE      TRUE
[73,]  FALSE     FALSE
[74,]   TRUE      TRUE
```

```
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[123,]  FALSE       TRUE
[124,]   TRUE       TRUE
[125,]  FALSE      FALSE
[126,]  FALSE      FALSE
[127,]  FALSE      FALSE
[128,]   TRUE      FALSE
```

```
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[133,]  TRUE  TRUE
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[178,]  TRUE  TRUE
[179,]  TRUE  TRUE
[180,]  TRUE  TRUE
[181,]  TRUE  TRUE
[182,]  TRUE  TRUE
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```
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[185,]  TRUE   FALSE
[186,] FALSE   FALSE
[187,]  TRUE    TRUE
[188,]  TRUE    TRUE
[189,] FALSE   FALSE
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[191,] FALSE   FALSE
[192,]  TRUE    TRUE
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[232,]  TRUE    TRUE
[233,]  TRUE    TRUE
[234,]  TRUE    TRUE
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[236,]  TRUE    TRUE
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[239,]   TRUE   FALSE
[240,]   TRUE    TRUE
[241,]   TRUE    TRUE
[242,]   TRUE    TRUE
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[244,]  FALSE   FALSE
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[251,]   TRUE    TRUE
[252,]   TRUE    TRUE
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[259,]   TRUE    TRUE
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[286,]   TRUE    TRUE
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[289,]  FALSE   FALSE
[290,]   TRUE   FALSE
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[291,]   TRUE       TRUE
[292,]   TRUE       TRUE
[293,]   TRUE       TRUE
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[296,]   TRUE       TRUE
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[329,]   TRUE       TRUE
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[343,]   TRUE       TRUE
[344,]  FALSE      FALSE
```

```
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[396,]   TRUE    TRUE
[397,]   TRUE    TRUE
[398,]   TRUE    TRUE
```

```
[399,] FALSE  FALSE
[400,]  TRUE   TRUE
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[403,]  TRUE   TRUE
[404,]  TRUE   TRUE
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[415,]  TRUE   TRUE
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[451,]  TRUE   TRUE
[452,] FALSE   TRUE
```

```
[453,]  FALSE     FALSE
[454,]  FALSE     FALSE
[455,]  FALSE     FALSE
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[472,]   TRUE      TRUE
[473,]  FALSE      TRUE
[474,]   TRUE      TRUE
[475,]   TRUE      TRUE
[476,]  FALSE     FALSE
[477,]   TRUE      TRUE
[478,]   TRUE      TRUE
[479,]  FALSE     FALSE
[480,]  FALSE     FALSE
[481,]   TRUE      TRUE
```

```
mean(apply(wtcfit6$predicted.match, 1, any))  #Fraction for which something is right
```

```
[1] 0.7941788
```

```
mean(apply(wtcfit6$predicted.match, 1, all))  #Fraction entirely right
```

```
[1] 0.6839917
```

```
colMeans(wtcfit6$predicted.match)  #Fraction src/target, respectively
```

```
   source recipient
0.7234927 0.7546778
```

Despite its simplicity, this model seems to fit extremely well. Further improvement is possible, but for many purposes we might view it as an adequate representation of the event dynamics in this WTC police network.

1.5 Simulating from the fitted model

In addition to fitting REMs, `relevent` has tools for simulating from them. These work a bit like the `simulate` commands in the `ergm` library, in that they can be used in two modes: we can simulate draws from a fitted `rem.dyad` model; or we can simulate draws from an *a priori* specified model. For now, let's consider this first case.

The syntax for the `rem.dyad` `simulate` method is as follows:

```
simulate(object, nsim = object$m, seed = NULL, coef = NULL, covar = NULL,
   verbose = FALSE, ...)
```

`object` here is our fitted model object, `nsim` is the number of events to draw from the model (the length of the event series to simulate), `seed` is an optional random number seed to specify, `coef` is a (here optional) coefficient vector, `covar` is our usual covariate list, and `verbose` says whether we want to print tracking information. By default, the coefficients used are taken from the fitted model, but specifying `coef` will allow them to be overridden (a useful tool for performing scenario analyses, as illustrated below). Likewise, the function will by default simulate as many events as were in the original data, but this can be altered by changing `nsim`. Note that we *do* have to specify any covariates being used when simulating, both because `rem.dyad` does not save the input covariates, and because (even if it did) the size of the covariate set in some cases depends on the number of events to be produced.

Let's begin with the most basic use case: simulating a synthetic replicate of our original data, using our final model. For this, we only need pass our model, and the covariates used:

```
set.seed(1331)
simwtc <- simulate(wtcfit6, covar = list(CovInt = WTCPoliceIsICR),
   verbose = TRUE)
```

```
Working on event 25 of 481
Working on event 50 of 481
Working on event 75 of 481
Working on event 100 of 481
Working on event 125 of 481
Working on event 150 of 481
Working on event 175 of 481
Working on event 200 of 481
Working on event 225 of 481
Working on event 250 of 481
Working on event 275 of 481
Working on event 300 of 481
Working on event 325 of 481
Working on event 350 of 481
Working on event 375 of 481
Working on event 400 of 481
Working on event 425 of 481
Working on event 450 of 481
Working on event 475 of 481
```

We now have a simulated event sequence from the `wtcfit6` model! Let's see what it looks like:

```
simwtc
```

```
               [,1] [,2] [,3]
  [1,] 0.0004468037   27   13
  [2,] 0.0004626364   13   27
  [3,] 0.0004704296   27   13
  [4,] 0.0004819716   13   27
  [5,] 0.0004923628   27   13
  [6,] 0.0005274594   13   27
  [7,] 0.0005329692   27   13
  [8,] 0.0005379387   13   27
  [9,] 0.0005687593   27   13
 [10,] 0.0006085596   13   27
 [11,] 0.0006466945   27   13
 [12,] 0.0006974054   13   27
 [13,] 0.0007084274   27   13
 [14,] 0.0007339464   13   27
 [15,] 0.0007466830   27   13
```

```
[16,] 0.0007492684   13   27
[17,] 0.0007884910   27   13
[18,] 0.0008027626   13   27
[19,] 0.0008181866   27   13
[20,] 0.0008316953   13   27
[21,] 0.0008386961   27   13
[22,] 0.0008486558   13   27
[23,] 0.0008972992   27   13
[24,] 0.0009089349   13   27
[25,] 0.0009255863   27   13
[26,] 0.0009356596   13   27
[27,] 0.0009481630   27   13
[28,] 0.0009701589   13   27
[29,] 0.0010908132   27   13
[30,] 0.0011515705   13   27
[31,] 0.0011593256   27   13
[32,] 0.0012039064   13   27
[33,] 0.0012429321   27   13
[34,] 0.0012671529   13   27
[35,] 0.0012826756   27   13
[36,] 0.0012830967   13   27
[37,] 0.0012937788   27   13
[38,] 0.0013168741   13   27
[39,] 0.0013233227   27   13
[40,] 0.0013545029   13   27
[41,] 0.0013680710   27   13
[42,] 0.0014074783   13   27
[43,] 0.0014247736   27   13
[44,] 0.0014539617   13   27
[45,] 0.0015243130   27   13
[46,] 0.0015514804   13   27
[47,] 0.0015694450   27   13
[48,] 0.0015723410   14    7
[49,] 0.0016150099    7   14
[50,] 0.0019005500   14    7
[51,] 0.0019436756   14    1
[52,] 0.0026720080   10   15
[53,] 0.0027797172   15   27
[54,] 0.0028284341   27   13
[55,] 0.0028393713   13   27
[56,] 0.0028778679   27   13
[57,] 0.0028872755   13   27
[58,] 0.0029061584   27   13
[59,] 0.0029642798   13   27
[60,] 0.0029984286   27   13
[61,] 0.0030100941   13   27
[62,] 0.0030511743   13   10
[63,] 0.0031090747   10   13
[64,] 0.0032220014   13   10
[65,] 0.0032321834   10   13
[66,] 0.0032814074   13   10
[67,] 0.0032917877   10   13
[68,] 0.0033707924   19   13
[69,] 0.0034818303   13   19
```

[70,]	0.0034824403	19	13
[71,]	0.0034995468	13	19
[72,]	0.0035038253	19	13
[73,]	0.0036111933	13	19
[74,]	0.0036167921	19	13
[75,]	0.0036274954	13	19
[76,]	0.0036565886	19	13
[77,]	0.0037396416	13	19
[78,]	0.0037581215	19	13
[79,]	0.0037626692	13	19
[80,]	0.0038189895	19	13
[81,]	0.0039261296	13	19
[82,]	0.0039629416	19	13
[83,]	0.0040927937	13	19
[84,]	0.0040931659	19	13
[85,]	0.0041057205	13	19
[86,]	0.0041215237	19	13
[87,]	0.0041289060	13	19
[88,]	0.0041427540	19	13
[89,]	0.0042120058	13	32
[90,]	0.0042217469	32	13
[91,]	0.0042779792	13	32
[92,]	0.0042783691	32	13
[93,]	0.0042967961	13	32
[94,]	0.0043393798	32	13
[95,]	0.0044448139	1	13
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[98,]	0.0048628324	27	13
[99,]	0.0049557731	13	27
[100,]	0.0049983478	27	13
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[102,]	0.0050738154	27	13
[103,]	0.0050807748	13	27
[104,]	0.0051075841	27	13
[105,]	0.0051297579	13	27
[106,]	0.0051722808	27	13
[107,]	0.0052835190	13	27
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[109,]	0.0053668581	13	27
[110,]	0.0053920783	27	13
[111,]	0.0053967363	13	27
[112,]	0.0053997402	27	13
[113,]	0.0054173586	13	27
[114,]	0.0054407510	27	13
[115,]	0.0054852012	13	27
[116,]	0.0054943325	27	13
[117,]	0.0055459602	13	27
[118,]	0.0055745360	27	13
[119,]	0.0055822403	13	27
[120,]	0.0055973214	22	19
[121,]	0.0056548129	7	16
[122,]	0.0056565788	7	32
[123,]	0.0057062083	32	7

[124,]	0.0058585216	7	32
[125,]	0.0058586075	19	27
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[133,]	0.0068017039	13	20
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```
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[195,] 0.0125951325   14   32
[196,] 0.0126633993    6   20
[197,] 0.0128275452   25   18
[198,] 0.0132555874    9    6
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[201,] 0.0134839250   36   13
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[213,] 0.0144495393   13   14
[214,] 0.0144640101   14   13
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[219,] 0.0145319757   13   14
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[229,] 0.0147680641    7   14
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[231,] 0.0151593357    7   14
```

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[253,]	0.0172588611	14	32
[254,]	0.0173394862	32	14
[255,]	0.0174859626	14	32
[256,]	0.0176055582	32	14
[257,]	0.0176171270	14	32
[258,]	0.0176355362	32	14
[259,]	0.0176363935	14	5
[260,]	0.0178551334	30	25
[261,]	0.0179038950	24	3
[262,]	0.0179614194	3	13
[263,]	0.0179934496	13	3
[264,]	0.0180305562	3	13
[265,]	0.0180429826	13	3
[266,]	0.0181813990	3	13
[267,]	0.0184782112	13	3
[268,]	0.0184845257	3	13
[269,]	0.0184972931	13	3
[270,]	0.0184988381	3	13
[271,]	0.0185055835	5	3
[272,]	0.0187918703	3	5
[273,]	0.0189023380	5	3
[274,]	0.0192145339	10	13
[275,]	0.0192505119	13	10
[276,]	0.0192688164	10	13
[277,]	0.0194784700	13	10
[278,]	0.0194887055	10	13
[279,]	0.0195002589	13	10
[280,]	0.0195378886	24	19
[281,]	0.0195719270	19	24
[282,]	0.0197782877	24	19
[283,]	0.0199081399	19	24
[284,]	0.0199500499	24	19
[285,]	0.0200982621	19	24

```
[286,] 0.0201604849   24   19
[287,] 0.0201623909   29   16
[288,] 0.0207869265   24   30
[289,] 0.0210273823   17   32
[290,] 0.0210622094   32   17
[291,] 0.0210828177   17   32
[292,] 0.0210952799   32   17
[293,] 0.0211329742   17   32
[294,] 0.0212798099   33   13
[295,] 0.0213271748   23    8
[296,] 0.0217965561    8   23
[297,] 0.0218333451   35   13
[298,] 0.0219790161   13   35
[299,] 0.0220608700   35   13
[300,] 0.0220865325   13   35
[301,] 0.0221579996   35   13
[302,] 0.0221665057   13   35
[303,] 0.0221694770   35   13
[304,] 0.0222068295   13   35
[305,] 0.0222089476   35   13
[306,] 0.0222403138    2   29
[307,] 0.0234768654    3   26
[308,] 0.0235433131   26    3
[309,] 0.0235718983   30   25
[310,] 0.0235745080   25   30
[311,] 0.0236604752   36   33
[312,] 0.0236673650   12   32
[313,] 0.0237699227   20   13
[314,] 0.0238429724   13    6
[315,] 0.0238765913    6   13
[316,] 0.0239138184   13    6
[317,] 0.0239983935    6   13
[318,] 0.0240305942   13    6
[319,] 0.0240332831    6   13
[320,] 0.0240570483   13    6
[321,] 0.0240782348    6   13
[322,] 0.0243157822   13    6
[323,] 0.0243718095    6   13
[324,] 0.0245154986   13    6
[325,] 0.0245408016    6   13
[326,] 0.0245484075   36   13
[327,] 0.0246745553   15   11
[328,] 0.0248603057   11   15
[329,] 0.0248915044   15   11
[330,] 0.0249525354   36   13
[331,] 0.0249679222   13   36
[332,] 0.0249824936   36   13
[333,] 0.0250038384   13   36
[334,] 0.0250310561   21   28
[335,] 0.0252419895    8   20
[336,] 0.0256013782   23    6
[337,] 0.0256986586   23   37
[338,] 0.0258426315   17   27
[339,] 0.0259477008   27   17
```

```
[340,] 0.0259488346   17   27
[341,] 0.0264904810   12   13
[342,] 0.0265228323   13   12
[343,] 0.0265818586   12   13
[344,] 0.0266614791    3   29
[345,] 0.0267612879   37   14
[346,] 0.0268845282   14   37
[347,] 0.0268879410   37   14
[348,] 0.0269286951   14   37
[349,] 0.0269360987   17    8
[350,] 0.0278964313    8   17
[351,] 0.0280965622   17    8
[352,] 0.0281559894    8   17
[353,] 0.0285467025    7   30
[354,] 0.0285679680   35   13
[355,] 0.0285992706   13   35
[356,] 0.0286171731   12   13
[357,] 0.0290322462   13   12
[358,] 0.0291357775   12   13
[359,] 0.0292442472   13   12
[360,] 0.0293683509   12   13
[361,] 0.0294945847   31   14
[362,] 0.0297095420   14   31
[363,] 0.0298376288   10   13
[364,] 0.0300455648   13   10
[365,] 0.0301098914   10   13
[366,] 0.0301205515   13   17
[367,] 0.0302045260    6    8
[368,] 0.0303020063    8    6
[369,] 0.0303115736    6    8
[370,] 0.0303131548   12   13
[371,] 0.0304611127   29    3
[372,] 0.0305443493    3   29
[373,] 0.0306824416   18   19
[374,] 0.0307545805    7   32
[375,] 0.0308680382   34   12
[376,] 0.0309930164   12   34
[377,] 0.0310660670   34   12
[378,] 0.0311366483   11   15
[379,] 0.0312986455   15   11
[380,] 0.0313265905   11   15
[381,] 0.0315919665   18   33
[382,] 0.0316031926   25   35
[383,] 0.0317072933   12   14
[384,] 0.0317276933   14   12
[385,] 0.0317654474   37   14
[386,] 0.0317947481   14   37
[387,] 0.0318287418   37   14
[388,] 0.0318921662   14   37
[389,] 0.0318968926   37   14
[390,] 0.0319175580   14   37
[391,] 0.0319322160   37   14
[392,] 0.0320606608   14   37
[393,] 0.0320616085   37   14
```

```
[394,] 0.0321529979   14   37
[395,] 0.0321957646   37   14
[396,] 0.0321971338   14   37
[397,] 0.0322595826   37   14
[398,] 0.0323020918   14   37
[399,] 0.0323578791   14   37
[400,] 0.0324794185   37   14
[401,] 0.0326005639   14   37
[402,] 0.0326094972   37   14
[403,] 0.0326346587   10   13
[404,] 0.0326597675   13   10
[405,] 0.0329174443   10   13
[406,] 0.0329720175   13   10
[407,] 0.0329972634   10   13
[408,] 0.0330169686   13   10
[409,] 0.0330238595   10   13
[410,] 0.0330583838   13   10
[411,] 0.0330733903   10   13
[412,] 0.0331370941    8   32
[413,] 0.0331712022   18   19
[414,] 0.0332798127   25    5
[415,] 0.0333958429    5   25
[416,] 0.0334240615   20    3
[417,] 0.0337391463   20   31
[418,] 0.0338543647   20   33
[419,] 0.0338626429   37   14
[420,] 0.0338645933   14   37
[421,] 0.0339029735   35   18
[422,] 0.0339429072   25    6
[423,] 0.0341417597   25    5
[424,] 0.0341505568   10   13
[425,] 0.0343134234   13   10
[426,] 0.0343159246   10   13
[427,] 0.0343269309   13   10
[428,] 0.0343773935   10   11
[429,] 0.0344291153   11   10
[430,] 0.0345942722    9   23
[431,] 0.0346363570   27   17
[432,] 0.0348390728   17   13
[433,] 0.0350104630   13   17
[434,] 0.0350182571   17   13
[435,] 0.0350464506    3   16
[436,] 0.0351329807   36   13
[437,] 0.0353440397   13   36
[438,] 0.0353784253   36   13
[439,] 0.0354021825   13   36
[440,] 0.0354351635   36   13
[441,] 0.0354445648   13   36
[442,] 0.0355089888   36   13
[443,] 0.0356242373   13   36
[444,] 0.0357127231   36   13
[445,] 0.0357545729   13   36
[446,] 0.0357551812   36   13
[447,] 0.0358335873   13   36
```

```
[448,] 0.0358677577   36   13
[449,] 0.0358935651    7   32
[450,] 0.0359377294   32    7
[451,] 0.0361369745    7   14
[452,] 0.0363378629   36   13
[453,] 0.0365084978   13   36
[454,] 0.0365349384    9   28
[455,] 0.0370825032   12   14
[456,] 0.0373067617   14   12
[457,] 0.0373914832   12   14
[458,] 0.0374009173   14   12
[459,] 0.0374550646   12   14
[460,] 0.0375279412   14   12
[461,] 0.0376051357   12   14
[462,] 0.0376379638   14   12
[463,] 0.0376565493   12   13
[464,] 0.0377125076   33   13
[465,] 0.0377720364   13   33
[466,] 0.0378468163   33   13
[467,] 0.0383414905   13   33
[468,] 0.0384142787   33   13
[469,] 0.0385017966   10   33
[470,] 0.0387486731   13    7
[471,] 0.0390431513   32   20
[472,] 0.0391026633   20   32
[473,] 0.0392090763   32   20
[474,] 0.0392492668   20   32
[475,] 0.0393944209   32   20
[476,] 0.0394789163   20   32
[477,] 0.0395283323   32   20
[478,] 0.0396423849   32   23
[479,] 0.0399125690   23   32
[480,] 0.0399974986   20   32
[481,] 0.0400171875    1   13
attr(,"n")
[1] 37
```

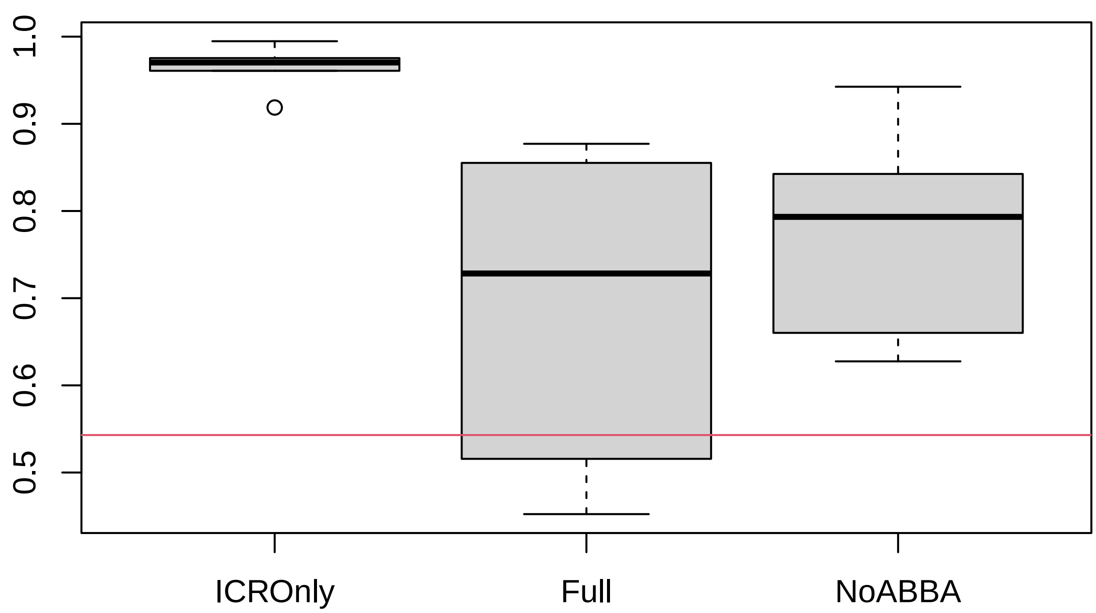
As we can see, we now have an event list that looks just like our original data (but that is synthetic). Such synthetic replicates can be used for many purposes, including exploratory simulation, model adequacy checking, and aiding in model interpretation. For instance, let's perform a very small simulation study to look at the relationship between occupying an ICR and betweenness, and probe the role of the AB-BA P-shift term in impacting that relationship. We'll do this by simulating data first from our ICR-only model, then our final model, and lastly a version of the final model with the P-shift term zeroed out. This is called an *in silico* "knock-out" experiment, and can be useful for understanding the role that specific effects play in generating aggregate outcomes.

```r
set.seed(1331)
reps <- 6  #Number of replicate series to take
kocoef <- wtcfit6$coef  #Knock-out coefs
kocoef["PSAB-BA"] <- 0
ICRBetCor <- matrix(nrow = reps, ncol = 3)
for (i in 1:reps) {
   print(i)
   simwtc <- simulate(wtcfit1, covar = list(CovInt = WTCPoliceIsICR))  #ICR only
   ICRBetCor[i, 1] <- cor(betweenness(as.sociomatrix.eventlist(simwtc,
```

```
      37)), WTCPoliceIsICR)
   simwtc <- simulate(wtcfit6, covar = list(CovInt = WTCPoliceIsICR))  #Final
   ICRBetCor[i, 2] <- cor(betweenness(as.sociomatrix.eventlist(simwtc,
      37)), WTCPoliceIsICR)
   simwtc <- simulate(wtcfit6, covar = list(CovInt = WTCPoliceIsICR),
      coef = kocoef)  #Knockout
   ICRBetCor[i, 3] <- cor(betweenness(as.sociomatrix.eventlist(simwtc,
      37)), WTCPoliceIsICR)
}
```

```
[1] 1
[1] 2
[1] 3
[1] 4
[1] 5
[1] 6
```

```
boxplot(ICRBetCor, names = c("ICROnly", "Full", "NoABBA"))
abline(h = cor(betweenness(as.sociomatrix.eventlist(WTCPoliceCalls,
   37)), WTCPoliceIsICR), col = 2)
```



We can see here that (perhaps unsurprisingly) the ICR-only model overstates the relationship between occupying an ICR and having high betweenness; our full model does much better, generally producing realizations that cover the observed data (though, with only a few replicates, you may find that it sometimes doesn't!). What happens when we "turn off" the AB-BA shift? It turns out that this greatly increases the relative betweenness of ICRs, telling us that the AB-BA shifts are helping to play a role in keeping ICRs from inappropriately dominating the network. Why should turn taking matter here? The short answer is that turn-taking effects create opportunities for non-ICR responders to gain airtime, and end up as emergent coordinators. Taking out the AB-BA effect reduces emergent coordination, which in turn increases the relative centrality of the few individuals in institutionalized coordinative roles.

Section 2. Dyadic Relational Event Models with `rem.dyad`: Exact Timing

In the previous section, we considered dyadic relational event models in the case for which only ordinal timing information is available. We now proceed to the case of exact timing, in which we know the time at which each event occurs (relative to the onset of observation, which is treated as time 0).

2.0 The McFarland classroom data

For this section, we will make use of data collected by Dan McFarland (and published in Bender-deMoll and McFarland, 2006) on interaction among students and instructors within a high school classroom. (Note that the data employed here has been slightly modified from the original for illustrative purposes, in that small timing adjustments have been made to separate closely spaced events; those interested in using it for purposes other than practice are directed to the above paper in the Journal of Social Structure.) To see the event data itself, we may print it as follows:

```
head(Class)
```

```
  StartTime FromId ToId
1     0.135     14   12
2     0.270     12   14
3     0.405     18   12
4     0.540     12   18
5     0.675      1   12
6     0.810     12    1
```

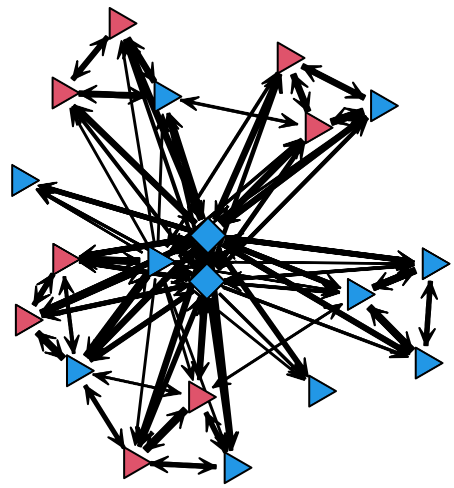
```
tail(Class)
```

```
    StartTime FromId ToId
687    50.426      1    3
688    50.547      3    1
689    50.668      6   17
690    50.789      6   17
691    50.910     17    6
692    50.920     NA   NA
```

As before, we have three columns: the event time, the event source (numbered from 1 to 20), and the event target (again, numbered 1 to 20). In this case, event time is given in increments of minutes from onset of observation. Note that the last row of the event list contains the time at which observation was terminated; it (and only it!) is allowed to contain `NA`s, since it has no meaning except to set the period during which events could have occurred. Where exact timing is used, the final entry in the edgelist is always interpreted in this way, and any source/target information on this row is ignored.

In addition to the `Class` edgelist, we also observe the covariates `ClassIsTeacher` (an indicator for instructor role) and `ClassIsFemale` (an indicator for gender). Visualizing the data in time-aggregate form gives us the following:

```
ClassNet <- as.sociomatrix.eventlist(Class, 20)
gplot(ClassNet, vertex.col = 4 - 2 * ClassIsFemale, vertex.sides = 3 +
   ClassIsTeacher, vertex.cex = 2, edge.lwd = ClassNet^0.75)
```



A dynamic visualization for this data is also available in the above-cited paper, and is well worth examining! (The `ndtv` package in `statnet` can be used to produce visualizations of this kind.)

2.1 Modeling with covariates

We begin our investigation of classroom dynamics with a trivial intercept model, containing only a vector of 1s (`ClassIntercept`) as a sending effect:

```
classfit1 <- rem.dyad(Class, n = 20, effects = c("CovSnd"), covar = list(CovSnd = ClassIntercept),
   ordinal = FALSE, hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```
summary(classfit1)
```

```
Relational Event Model (Temporal Likelihood)

          Estimate   Std.Err Z value  Pr(>|z|)
CovSnd.1 -3.332287  0.038042 -87.596 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 5987.221 on 691 degrees of freedom
Residual deviance: 5987.221 on 691 degrees of freedom
    Chi-square: -3.728928e-11 on 0 degrees of freedom, asymptotic p-value 1
```

```
AIC: 5989.221 AICC: 5989.227 BIC: 5993.759
```

Note that we must tell `rem.dyad` that we do not want to discard timing information (`ordinal=FALSE`). The model does not fit any better than the null because it is equivalent to the null model (but you must supply your own intercept, regardless!). As one would expect from first principles, this is really just an exponential waiting time model, calibrated to the observed communication rate:

```
(classfit1$m - 1)/max(Class[, 1])  #Events per minute (on average)
```

```
[1] 13.57031
```

```
20 * 19 * exp(classfit1$coef)  #Predicted events per minute (matches well!)
```

```
CovSnd.1
13.57031
```

To make things more interesting, let's add effects for role and gender:

```
classfit2 <- rem.dyad(Class, n = 20, effects = c("CovSnd", "CovRec"),
   covar = list(CovSnd = cbind(ClassIntercept, ClassIsTeacher,
      ClassIsFemale), CovRec = cbind(ClassIsTeacher, ClassIsFemale)),
   ordinal = FALSE, hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```
summary(classfit2)
```

```
Relational Event Model (Temporal Likelihood)

          Estimate   Std.Err  Z value  Pr(>|z|)
CovSnd.1 -3.834216  0.078841 -48.6320 < 2.2e-16 ***
CovSnd.2  1.672539  0.091679  18.2434 < 2.2e-16 ***
CovSnd.3  0.123880  0.094931   1.3049  0.191911
CovRec.1  0.373750  0.127027   2.9423  0.003258 **
CovRec.2  0.165734  0.080896   2.0487  0.040488 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 5987.221 on 691 degrees of freedom
Residual deviance: 5652.318 on 687 degrees of freedom
    Chi-square: 334.9034 on 4 degrees of freedom, asymptotic p-value 0
AIC: 5662.318 AICC: 5662.405 BIC: 5685.008
```

```
classfit1$BIC - classfit2$BIC  #Model is preferred
```

```
[1] 308.7508
```

Note that covariate effects correspond to the order in which they were specified within the covar argument. It doesn't look here like gender affects propensity to send; given this, we might wonder whether dropping it gives us a better model.

```
classfit3 <- rem.dyad(Class, n = 20, effects = c("CovSnd", "CovRec"),
   covar = list(CovSnd = cbind(ClassIntercept, ClassIsTeacher),
      CovRec = cbind(ClassIsTeacher, ClassIsFemale)), ordinal = FALSE,
   hessian = TRUE)
```

```
Prepping edgelist.
```

```
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```r
summary(classfit3)
```

```
Relational Event Model (Temporal Likelihood)

          Estimate   Std.Err  Z value  Pr(>|z|)
CovSnd.1 -3.775222  0.063622 -59.3380 < 2.2e-16 ***
CovSnd.2  1.615759  0.079933  20.2139 < 2.2e-16 ***
CovRec.1  0.371765  0.127019   2.9268  0.003424 **
CovRec.2  0.161158  0.080815   1.9942  0.046135 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 5987.221 on 691 degrees of freedom
Residual deviance: 5654.016 on 688 degrees of freedom
    Chi-square: 333.2049 on 3 degrees of freedom, asymptotic p-value 0
AIC: 5662.016 AICC: 5662.074 BIC: 5680.169
```

```r
classfit2$BIC - classfit3$BIC  #Reduced model is indeed preferred
```

```
[1] 4.83966
```

2.2 Endogenous social dynamics

The above model is still relatively poor, in the sense that the reduction in deviance is unimpressive. What else might explain classroom communication? Recency effects would seem to be a reasonable bet:

```r
classfit4 <- rem.dyad(Class, n = 20, effects = c("CovSnd", "CovRec",
   "RRecSnd", "RSndSnd"), covar = list(CovSnd = cbind(ClassIntercept,
   ClassIsTeacher), CovRec = cbind(ClassIsTeacher, ClassIsFemale)),
   ordinal = FALSE, hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```r
summary(classfit4)
```

```
Relational Event Model (Temporal Likelihood)

          Estimate   Std.Err  Z value  Pr(>|z|)
RRecSnd   4.153303  0.119899  34.6399 < 2.2e-16 ***
RSndSnd  -1.399534  0.133148 -10.5111 < 2.2e-16 ***
CovSnd.1 -4.467621  0.075244 -59.3749 < 2.2e-16 ***
CovSnd.2  1.448498  0.080958  17.8921 < 2.2e-16 ***
CovRec.1 -1.364388  0.139346  -9.7914 < 2.2e-16 ***
CovRec.2  0.270110  0.083327   3.2416  0.001189 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 5987.221 on 691 degrees of freedom
Residual deviance: 4522.646 on 686 degrees of freedom
    Chi-square: 1464.575 on 5 degrees of freedom, asymptotic p-value 0
```

```
AIC: 4534.646 AICC: 4534.769 BIC: 4561.875
```

```r
classfit3$BIC - classfit4$BIC  #Enhanced model is preferred
```

```
[1] 1118.294
```

This certainly helps, but we may suspect that more structure is present. Although a classroom is not as structured as a radio channel, we might reasonably expect to see at least modest adherence to conversational norms such as turn-taking. Moreover, sequential address and "hand-offs" might also be expected to occur more frequently here than would be expected by chance. To examine these possibilities, we incorporate the appropriate P-shift effects into our cumulative model:

```r
classfit5 <- rem.dyad(Class, n = 20, effects = c("CovSnd", "CovRec",
   "RRecSnd", "RSndSnd", "PSAB-BA", "PSAB-AY", "PSAB-BY"), covar = list(CovSnd = cbind(ClassIntercept,
   ClassIsTeacher), CovRec = cbind(ClassIsTeacher, ClassIsFemale)),
   ordinal = FALSE, hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```r
summary(classfit5)
```

```
Relational Event Model (Temporal Likelihood)

          Estimate   Std.Err  Z value  Pr(>|z|)
RRecSnd   2.429251  0.155364  15.6359 < 2.2e-16 ***
RSndSnd  -0.986754  0.144667  -6.8209  9.05e-12 ***
CovSnd.1 -5.003435  0.090609 -55.2202 < 2.2e-16 ***
CovSnd.2  1.253899  0.085160  14.7240 < 2.2e-16 ***
CovRec.1 -0.722678  0.141949  -5.0911  3.56e-07 ***
CovRec.2  0.047945  0.081325   0.5896    0.5555
PSAB-BA   4.622101  0.137599  33.5910 < 2.2e-16 ***
PSAB-BY   1.677566  0.164931  10.1713 < 2.2e-16 ***
PSAB-AY   2.869963  0.103113  27.8332 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 5987.221 on 691 degrees of freedom
Residual deviance: 2803.315 on 683 degrees of freedom
    Chi-square: 3183.906 on 8 degrees of freedom, asymptotic p-value 0
AIC: 2821.315 AICC: 2821.58 BIC: 2862.158
```

```r
classfit4$BIC - classfit5$BIC  #Enhanced model is again preferred
```

```
[1] 1699.716
```

Note that, while P-shift effects are certainly present, including them has led the remaining gender effect to fall out. This suggests the possibility that what seemed at first to be a difference in communication receipt tendency by gender was in fact a result of social dynamics (perhaps stemming from the fact that the instructors are male, with their inherent tendency to communicate more often amplified by local conversational norms). Does dropping gender now result in improved model fit? Let's check.

```r
set.seed(13)  #To ensure that our later results can be reproduced
classfit6 <- rem.dyad(Class, n = 20, effects = c("CovSnd", "CovRec",
   "RRecSnd", "RSndSnd", "PSAB-BA", "PSAB-AY", "PSAB-BY"), covar = list(CovSnd = cbind(ClassIntercept,
   ClassIsTeacher), CovRec = ClassIsTeacher), ordinal = FALSE,
```

```
   hessian = TRUE)
```

```
Prepping edgelist.
Checking/prepping covariates.
Computing preliminary statistics
Fitting model
Obtaining goodness-of-fit statistics
```

```
summary(classfit6)
```

```
Relational Event Model (Temporal Likelihood)

          Estimate   Std.Err  Z value  Pr(>|z|)
RRecSnd   2.430697  0.155292  15.6524 < 2.2e-16 ***
RSndSnd  -0.984633  0.144654  -6.8068 9.979e-12 ***
CovSnd.1 -4.983918  0.084196 -59.1943 < 2.2e-16 ***
CovSnd.2  1.257292  0.084967  14.7975 < 2.2e-16 ***
CovRec.1 -0.745119  0.136612  -5.4543 4.917e-08 ***
PSAB-BA   4.623684  0.137503  33.6261 < 2.2e-16 ***
PSAB-BY   1.677832  0.164940  10.1724 < 2.2e-16 ***
PSAB-AY   2.870517  0.103103  27.8411 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Null deviance: 5987.221 on 691 degrees of freedom
Residual deviance: 2803.662 on 684 degrees of freedom
    Chi-square: 3183.558 on 7 degrees of freedom, asymptotic p-value 0
AIC: 2819.662 AICC: 2819.874 BIC: 2855.968
```

```
classfit5$AICC - classfit6$AICC  #Reduced model is indeed preferred
```

```
[1] 1.705912
```

At this point, we have a relatively simple model that incorporates some plausible social mechanisms. We could continue to elaborate it, but for instructional purposes we stop our search here.

2.3 Using a fitted model to investigate event timing

One use of a fitted relational event model is to consider the inter-event times predicted to be observed under various scenarios. For this purpose, it is useful to remember that, under the piecewise constant hazard assumption, event waiting times are conditionally exponentially distributed. This allows us to easily work out the consequences of various model effects for social dynamics, at least within the context of a particular scenario.

In interpreting coefficient effects, recall that they act as logged hazard multipliers. For instance:

```
exp(classfit6$coef["PSAB-BA"])  #Response events have apx 100 times the hazard of other events
```

```
 PSAB-BA
101.8686
```

Remember, however, that the fact that an event has an unusually high hazard does not mean that it will necessarily occur. For instance, while a response of B to a communication from A has a hazard that is (*ceteris paribus*) about 100 times as great as the hazard of a non B→A event, there are many more events of the latter type. Here, indeed, there are 379 other events "competing" with the B→A response, and thus the chance that the latter will occur next is smaller than it may appear. Both relative rates and combinatorics (i.e., the number of possible ways that an event type may occur) govern the result.

One basic use of the model coefficients is to examine the expected inter-event times under specific scenarios. E.g.:

```
# Mean inter-event time if nothing else going on....
1/(20 * 19 * exp(classfit6$coef["CovSnd.1"]))
```

```
 CovSnd.1
0.3843301
```

```
# Mean teacher-student time (again, if nothing else
# happened)
1/(2 * 18 * exp(sum(classfit6$coef[c("CovSnd.1", "CovSnd.2")])))
```

```
[1] 1.153853
```

```
# Sequential address by teacher w/out prior interaction,
# given a prior teacher-student interaction, and assuming
# nothing else happened
1/(17 * exp(sum(classfit6$coef[c("CovSnd.1", "CovSnd.2", "PSAB-AY")])))
```

```
[1] 0.1384696
```

```
# Teacher responding to a specific student, given an
# immediate event
1/(exp(sum(classfit6$coef[c("CovSnd.1", "CovSnd.2", "PSAB-BA",
   "RRecSnd")])))
```

```
[1] 0.03587354
```

```
# Student responding to a specific teacher, given an
# immediate event
1/(exp(sum(classfit6$coef[c("CovSnd.1", "CovRec.1", "PSAB-BA",
   "RRecSnd")])))
```

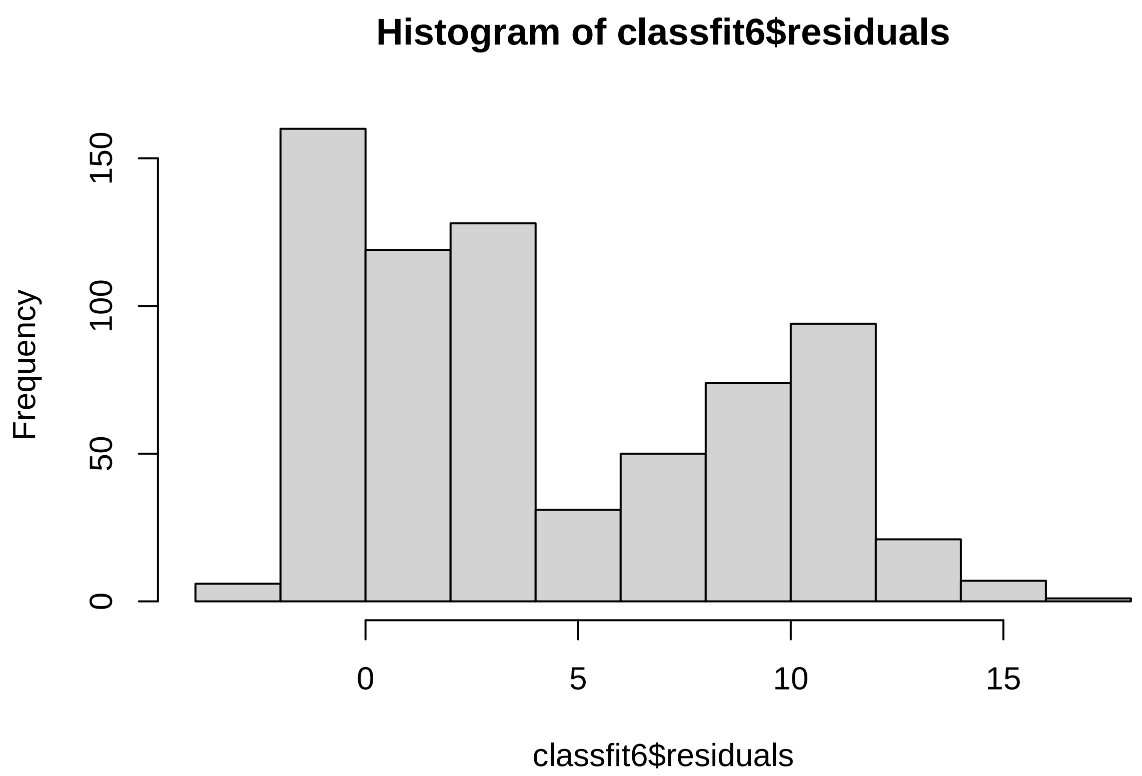
```
[1] 0.2657116
```

Again, the number of ways that an event type can occur and the propensity of such events to occur both matter!

2.4 Assessing model adequacy

Model adequacy assessment in the exact timing case is much like that of the ordinal case. We cannot here use a fixed null residual or guessing equivalent, but can still look at "surprise" based on deviance residuals:

```
# Where is the model 'surprised'? Can't use null residual
# trick, but can see what the distribution looks like
hist(classfit6$residuals)  #Deviance residuals - lumpier by far, most smallish
```



The fit here doesn't seem to be as good as it was for the WTC police data. Let's look at classification:

```
mean(apply(classfit6$predicted.match, 1, all))  #Exactly right about 33%
```

```
[1] 0.3299566
```

```
mean(apply(classfit6$predicted.match, 1, any))  #Get one party exactly right 52%
```

```
[1] 0.5166425
```

```
colMeans(classfit6$predicted.match)  #Better at sender than receiver!
```

```
   FromId      ToId
0.5050651 0.3415340
```

```
classfit6$observed.rank
```

```
  [1]   1   1  58   1  77   1  39   1   3   4   4   4   4   4  19   4   4   4
 [19]   4   3   3   4   4   1   3   4   4  54   3   3   3   3   3   3   3   3
 [37]   3   3   3   2   2   3   3   3   3   3  92   1   5   1   4   1   4   1
 [55]   4   1  40   1  65   6  11   9  20   7   8   4  10  99   1   1   1  59
 [73]   3   3  14  14   3   3   3  12   3  10   3   2   2   3   3   3   3   3
 [91]  23   1   3   4   4   4   4   4   4   4   4   4   4   4   3   3   4   1
[109]   3   4   4 374   1 110   1  59   4   4   4   4   4   4   4   4   4   4
[127]   4   3   3   4   1   3   4   4 106   1 123   1  60   4   4   4   4   4
[145]   4   4   4   4   4   4   3   3   4   1   3   4   4 111   8   8   5   7
[163]   2  10   8   6   7   3   7   7  14   8   8   8   8   8 122   1 125   1
[181] 115   1 130   1  86   2  10   1  29   1  47   1 115   1 110   1  48   1
[199]   1   1  61   1  36   1   8   1   8   1 130   1   1   1 133   1  50   1
```

```
[217]  89   1  98   2   4   2  33   1 119   1  94   1  51   1 122   1   2   1
[235]   2   1  50   1 117   1  51   1   3   1 131   1  88   1  27   1  32   1
[253]  74   1  53   1 119   1 121   1  52   1  52   1  91   1 128   1  54   1
[271]  92   1   2   1  94   1  92   1 120   1 128   1  53   1  52   1  25   1
[289]  24   1  94   1  92   1  52   1  92   1  52   1 113   1  70   9   9   8
[307]   8   3   8   9   9   1   8   9  19   4   4   4   8   9   6  55  10  10
[325]   4   4  10   2  10   7   3   9   6  10  11  11  10   9   9   9 113   1
[343] 129   1 368   1 120   1 371   1 110   1  24   1  51   1   9   2  10   2
[361]  49   1 119   1 123   1 108   1 120   1 118   1 129   1   4   1  55   1
[379]  94  89   1  13   1  32   1  74   1   4   1  58   1 111   1 103  92   1
[397]   4   1  97   1  58   1  56   1 128   1   1   1  19   1   2   2   4   2
[415] 379   1 369   1  92   1 127   1  52   1 112   1  79   1  32   1  30   1
[433]  72   1  53   1   2   1 133   1  92   1 113   1  52   1  53   1  54   1
[451]  54   1  73   1  31   1  34   1  70   1 138   1 116   1 127   1  55   1
[469]   3   1   2   1  91   1  55   1  91   1  83   1  15   1  35   1  70   1
[487] 116   1  54   1  89   1 114   1   3   1 114   1  83   1  17   1  21   1
[505]  20   1  64   1  12   2  20   1  98   1  53   1  53   1  44   2   8   2
[523]   9   2  66   1 114   1  86   1  88   1 109   1 112   1  78   2  19   1
[541]  19   1  47   1  88   1 110   1  89   1 119   1  77   2  19   2  19   2
[559]  94   1   2   1 112  52   1 121   1   2   1 134   1  87   1 125   1  53
[577]   1  72   1  18   1  17   1  18   1   5   1  53   1 125 123   1  90   1
[595] 111   1  77   2  19   1  20   2  48   1  86   1  54   1  88   1 112   1
[613]   1   1  89   1 114   1 132   2   1  80   1  14   2  19   2  72   1  89
[631]   1  53   1  54   1  54   1  89   1   3   1  45   2   8   2   8   2  10
[649]   2 106   1 122  52   1  91   1  53   1 115   1  53   1  91   1  47   2
[667]   2  17  17  13  12   6  13   5   9   5  10  10  19   2   8   7   4  15
[685]   8  59  22   1 142 380   1
```

```
cbind(Class, c(classfit6$observed.rank, NA))
```

```
   StartTime FromId ToId c(classfit6$observed.rank, NA)
1      0.135     14   12                              1
2      0.270     12   14                              1
3      0.405     18   12                             58
4      0.540     12   18                              1
5      0.675      1   12                             77
6      0.810     12    1                              1
7      0.945     14   17                             39
8      1.080     17   14                              1
9      1.257     14    1                              3
10     1.267     14    2                              4
11     1.277     14    3                              4
12     1.287     14    4                              4
13     1.297     14    5                              4
14     1.307     14    6                              4
15     1.317     14    7                             19
16     1.327     14    8                              4
17     1.337     14    9                              4
18     1.347     14   10                              4
19     1.357     14   11                              4
20     1.367     14   12                              3
21     1.377     14   13                              3
22     1.387     14   15                              4
23     1.397     14   16                              4
24     1.407     14   17                              1
```

25	1.417	14	18	3
26	1.427	14	19	4
27	1.437	14	20	4
28	1.613	7	1	54
29	1.623	7	2	3
30	1.633	7	3	3
31	1.643	7	4	3
32	1.653	7	5	3
33	1.663	7	6	3
34	1.673	7	8	3
35	1.683	7	9	3
36	1.693	7	10	3
37	1.703	7	11	3
38	1.713	7	12	3
39	1.723	7	13	3
40	1.733	7	14	2
41	1.743	7	15	2
42	1.753	7	16	3
43	1.763	7	17	3
44	1.773	7	18	3
45	1.783	7	19	3
46	1.793	7	20	3
47	1.970	4	12	92
48	2.147	12	4	1
49	2.323	12	10	5
50	2.500	10	12	1
51	2.677	10	4	4
52	2.853	4	10	1
53	3.030	4	5	4
54	3.207	5	4	1
55	3.383	5	10	4
56	3.560	10	5	1
57	3.737	5	12	40
58	3.913	12	5	1
59	4.090	7	4	65
60	4.267	7	5	6
61	4.443	7	12	11
62	4.620	7	10	9
63	4.797	14	7	20
64	4.973	14	4	7
65	5.150	14	5	8
66	5.327	14	12	4
67	5.503	14	10	10
68	5.680	16	17	99
69	5.857	17	16	1
70	6.033	16	17	1
71	6.210	17	16	1
72	6.387	7	1	59
73	6.397	7	2	3
74	6.407	7	3	3
75	6.417	7	4	14
76	6.427	7	5	14
77	6.437	7	6	3
78	6.447	7	8	3

79	6.457	7	9	3
80	6.467	7	10	12
81	6.477	7	11	3
82	6.487	7	12	10
83	6.497	7	13	3
84	6.507	7	14	2
85	6.517	7	15	2
86	6.527	7	16	3
87	6.537	7	17	3
88	6.547	7	18	3
89	6.557	7	19	3
90	6.567	7	20	3
91	6.743	17	7	23
92	6.920	7	17	1
93	7.037	7	1	3
94	7.047	7	2	4
95	7.057	7	3	4
96	7.067	7	4	4
97	7.077	7	5	4
98	7.087	7	6	4
99	7.097	7	8	4
100	7.107	7	9	4
101	7.117	7	10	4
102	7.127	7	11	4
103	7.137	7	12	4
104	7.147	7	13	4
105	7.157	7	14	3
106	7.167	7	15	3
107	7.177	7	16	4
108	7.187	7	17	1
109	7.197	7	18	3
110	7.207	7	19	4
111	7.217	7	20	4
112	7.334	10	5	374
113	7.451	5	10	1
114	7.569	4	12	110
115	7.686	12	4	1
116	7.803	7	1	59
117	7.813	7	2	4
118	7.823	7	3	4
119	7.833	7	4	4
120	7.843	7	5	4
121	7.853	7	6	4
122	7.863	7	8	4
123	7.873	7	9	4
124	7.883	7	10	4
125	7.893	7	11	4
126	7.903	7	12	4
127	7.913	7	13	4
128	7.923	7	14	3
129	7.933	7	15	3
130	7.943	7	16	4
131	7.953	7	17	1
132	7.963	7	18	3

133	7.973	7	19	4
134	7.983	7	20	4
135	8.100	18	1	106
136	8.217	1	18	1
137	8.334	20	17	123
138	8.451	17	20	1
139	8.569	7	1	60
140	8.579	7	2	4
141	8.589	7	3	4
142	8.599	7	4	4
143	8.609	7	5	4
144	8.619	7	6	4
145	8.629	7	8	4
146	8.639	7	9	4
147	8.649	7	10	4
148	8.659	7	11	4
149	8.669	7	12	4
150	8.679	7	13	4
151	8.689	7	14	3
152	8.699	7	15	3
153	8.709	7	16	4
154	8.719	7	17	1
155	8.729	7	18	3
156	8.739	7	19	4
157	8.749	7	20	4
158	8.866	4	1	111
159	8.876	4	2	8
160	8.886	4	3	8
161	8.896	4	5	5
162	8.906	4	6	7
163	8.916	4	7	2
164	8.926	4	8	10
165	8.936	4	9	8
166	8.946	4	10	6
167	8.956	4	11	7
168	8.966	4	12	3
169	8.976	4	13	7
170	8.986	4	14	7
171	8.996	4	15	14
172	9.006	4	16	8
173	9.016	4	17	8
174	9.026	4	18	8
175	9.036	4	19	8
176	9.046	4	20	8
177	9.163	16	20	122
178	9.280	20	16	1
179	9.397	9	18	125
180	9.514	18	9	1
181	9.631	20	17	115
182	9.749	17	20	1
183	9.866	13	3	130
184	9.983	3	13	1
185	10.100	14	18	86
186	10.217	18	14	2

187	10.334	14	1	10
188	10.451	1	14	1
189	10.569	14	9	29
190	10.686	9	14	1
191	10.803	10	4	47
192	10.920	4	10	1
193	11.037	18	1	115
194	11.154	1	18	1
195	11.271	4	5	110
196	11.389	5	4	1
197	11.506	18	1	48
198	11.623	1	18	1
199	11.740	18	1	1
200	11.857	1	18	1
201	11.974	14	12	61
202	12.091	12	14	1
203	12.209	14	5	36
204	12.326	5	14	1
205	12.443	14	4	8
206	12.560	4	14	1
207	12.677	4	12	8
208	12.794	12	4	1
209	12.911	11	15	130
210	13.029	15	11	1
211	13.146	11	15	1
212	13.263	15	11	1
213	13.380	8	13	133
214	13.497	13	8	1
215	13.614	20	17	50
216	13.731	17	20	1
217	13.849	14	10	89
218	13.966	10	14	1
219	14.083	7	20	98
220	14.200	20	7	2
221	14.317	7	17	4
222	14.434	17	7	2
223	14.551	7	16	33
224	14.669	16	7	1
225	14.786	1	9	119
226	14.903	9	1	1
227	15.020	13	3	94
228	15.137	3	13	1
229	15.254	11	15	51
230	15.371	15	11	1
231	15.489	12	10	122
232	15.606	10	12	1
233	15.723	10	4	2
234	15.840	4	10	1
235	15.957	4	12	2
236	16.074	12	4	1
237	16.191	10	4	50
238	16.309	4	10	1
239	16.426	17	16	117
240	16.543	16	17	1

241	16.660	1	9	51
242	16.777	9	1	1
243	16.894	9	18	3
244	17.011	18	9	1
245	17.129	3	8	131
246	17.246	8	3	1
247	17.363	7	15	88
248	17.480	15	7	1
249	17.597	7	6	27
250	17.714	6	7	1
251	17.831	7	11	32
252	17.949	11	7	1
253	18.066	12	10	74
254	18.183	10	12	1
255	18.300	17	16	53
256	18.417	16	17	1
257	18.534	4	5	119
258	18.651	5	4	1
259	18.769	12	5	121
260	18.886	5	12	1
261	19.003	4	5	52
262	19.120	5	4	1
263	19.237	13	3	52
264	19.354	3	13	1
265	19.471	18	1	91
266	19.589	1	18	1
267	19.706	6	11	128
268	19.823	11	6	1
269	19.940	13	3	54
270	20.057	3	13	1
271	20.174	10	4	92
272	20.291	4	10	1
273	20.409	4	5	2
274	20.526	5	4	1
275	20.643	3	8	94
276	20.760	8	3	1
277	20.877	20	17	92
278	20.994	17	20	1
279	21.111	5	10	120
280	21.229	10	5	1
281	21.346	15	6	128
282	21.463	6	15	1
283	21.580	12	5	53
284	21.697	5	12	1
285	21.814	4	5	52
286	21.931	5	4	1
287	22.049	4	12	25
288	22.166	12	4	1
289	22.283	4	5	24
290	22.400	5	4	1
291	22.517	8	13	94
292	22.634	13	8	1
293	22.751	17	16	92
294	22.869	16	17	1

295	22.986	3	8	52
296	23.103	8	3	1
297	23.220	4	12	92
298	23.337	12	4	1
299	23.454	3	8	52
300	23.571	8	3	1
301	23.689	5	10	113
302	23.806	10	5	1
303	23.923	7	1	70
304	23.933	7	2	9
305	23.943	7	3	9
306	23.953	7	4	8
307	23.963	7	5	8
308	23.973	7	6	3
309	23.983	7	8	8
310	23.993	7	9	9
311	24.003	7	10	9
312	24.013	7	11	1
313	24.023	7	12	8
314	24.033	7	13	9
315	24.043	7	14	19
316	24.053	7	15	4
317	24.063	7	16	4
318	24.073	7	17	4
319	24.083	7	18	8
320	24.093	7	19	9
321	24.103	7	20	6
322	24.220	14	1	55
323	24.230	14	2	10
324	24.240	14	3	10
325	24.250	14	4	4
326	24.260	14	5	4
327	24.270	14	6	10
328	24.280	14	7	2
329	24.290	14	8	10
330	24.300	14	9	7
331	24.310	14	10	3
332	24.320	14	11	9
333	24.330	14	12	6
334	24.340	14	13	10
335	24.350	14	15	11
336	24.360	14	16	11
337	24.370	14	17	10
338	24.380	14	18	9
339	24.390	14	19	9
340	24.400	14	20	9
341	24.480	10	4	113
342	24.560	4	10	1
343	24.639	8	13	129
344	24.719	13	8	1
345	24.799	18	1	368
346	24.879	1	18	1
347	24.958	12	18	120
348	25.038	18	12	1

349	25.118	3	8	371
350	25.198	8	3	1
351	25.277	20	16	110
352	25.357	16	20	1
353	25.437	20	4	24
354	25.517	4	20	1
355	25.597	14	9	51
356	25.676	9	14	1
357	25.756	14	1	9
358	25.836	1	14	2
359	25.916	14	18	10
360	25.995	18	14	2
361	26.075	10	4	49
362	26.155	4	10	1
363	26.235	1	9	119
364	26.314	9	1	1
365	26.394	4	12	123
366	26.474	12	4	1
367	26.554	18	1	108
368	26.633	1	18	1
369	26.713	12	10	120
370	26.793	10	12	1
371	26.873	9	18	118
372	26.953	18	9	1
373	27.032	16	17	129
374	27.112	17	16	1
375	27.192	17	20	4
376	27.272	20	17	1
377	27.351	3	8	55
378	27.431	8	3	1
379	27.511	20	4	94
380	27.591	7	18	89
381	27.670	18	7	1
382	27.750	7	1	13
383	27.830	1	7	1
384	27.910	7	9	32
385	27.990	9	7	1
386	28.069	8	13	74
387	28.149	13	8	1
388	28.229	13	3	4
389	28.309	3	13	1
390	28.388	16	17	58
391	28.468	17	16	1
392	28.548	12	18	111
393	28.628	18	12	1
394	28.707	17	4	103
395	28.787	9	18	92
396	28.867	18	9	1
397	28.947	18	1	4
398	29.027	1	18	1
399	29.106	10	4	97
400	29.186	4	10	1
401	29.266	18	1	58
402	29.346	1	18	1

403	29.425	13	3	56
404	29.505	3	13	1
405	29.585	6	11	128
406	29.665	11	6	1
407	29.744	6	11	1
408	29.824	11	6	1
409	29.904	14	18	19
410	29.984	18	14	1
411	30.063	14	1	2
412	30.143	1	14	2
413	30.223	14	9	4
414	30.303	9	14	2
415	30.383	17	4	379
416	30.462	4	17	1
417	30.542	15	6	369
418	30.622	6	15	1
419	30.702	12	10	92
420	30.781	10	12	1
421	30.861	4	12	127
422	30.941	12	4	1
423	31.021	13	3	52
424	31.100	3	13	1
425	31.180	20	16	112
426	31.260	16	20	1
427	31.340	14	11	79
428	31.420	11	14	1
429	31.499	14	15	32
430	31.579	15	14	1
431	31.659	14	6	30
432	31.739	6	14	1
433	31.818	15	6	72
434	31.898	6	15	1
435	31.978	4	12	53
436	32.058	12	4	1
437	32.137	12	10	2
438	32.217	10	12	1
439	32.297	5	4	133
440	32.377	4	5	1
441	32.457	3	8	92
442	32.536	8	3	1
443	32.616	17	20	113
444	32.696	20	17	1
445	32.776	15	6	52
446	32.855	6	15	1
447	32.935	3	8	53
448	33.015	8	3	1
449	33.095	13	3	54
450	33.174	3	13	1
451	33.254	17	20	54
452	33.334	20	17	1
453	33.414	7	3	73
454	33.493	3	7	1
455	33.573	7	8	31
456	33.653	8	7	1

457	33.733	7	13	34
458	33.813	13	7	1
459	33.892	16	17	70
460	33.972	17	16	1
461	34.052	5	10	138
462	34.132	10	5	1
463	34.211	6	11	116
464	34.291	11	6	1
465	34.371	1	9	127
466	34.451	9	1	1
467	34.530	6	11	55
468	34.610	11	6	1
469	34.690	11	15	3
470	34.770	15	11	1
471	34.850	15	6	2
472	34.929	6	15	1
473	35.009	20	16	91
474	35.089	16	20	1
475	35.169	11	15	55
476	35.248	15	11	1
477	35.328	5	4	91
478	35.408	4	5	1
479	35.488	14	16	83
480	35.567	16	14	1
481	35.647	14	17	15
482	35.727	17	14	1
483	35.807	14	20	35
484	35.887	20	14	1
485	35.966	5	10	70
486	36.046	10	5	1
487	36.126	16	17	116
488	36.206	17	16	1
489	36.285	12	10	54
490	36.365	10	12	1
491	36.445	20	16	89
492	36.525	16	20	1
493	36.604	10	4	114
494	36.684	4	10	1
495	36.764	4	12	3
496	36.844	12	4	1
497	36.923	17	20	114
498	37.003	20	17	1
499	37.083	7	12	83
500	37.163	12	7	1
501	37.243	7	4	17
502	37.322	4	7	1
503	37.402	7	5	21
504	37.482	5	7	1
505	37.562	7	10	20
506	37.641	10	7	1
507	37.721	14	13	64
508	37.801	13	14	1
509	37.881	14	1	12
510	37.960	1	14	2

511	38.040	14	3	20
512	38.120	3	14	1
513	38.196	4	10	98
514	38.272	10	4	1
515	38.347	10	4	53
516	38.423	4	10	1
517	38.499	11	15	53
518	38.575	15	11	1
519	38.651	14	20	44
520	38.726	20	14	2
521	38.802	14	17	8
522	38.878	17	14	2
523	38.954	14	16	9
524	39.029	16	14	2
525	39.105	5	10	66
526	39.181	10	5	1
527	39.257	13	3	114
528	39.333	3	13	1
529	39.408	17	20	86
530	39.484	20	17	1
531	39.560	6	11	88
532	39.636	11	6	1
533	39.712	4	12	109
534	39.787	12	4	1
535	39.863	9	18	112
536	39.939	18	9	1
537	40.015	7	16	78
538	40.091	16	7	2
539	40.166	7	20	19
540	40.242	20	7	1
541	40.318	7	17	19
542	40.394	17	7	1
543	40.469	6	11	47
544	40.545	11	6	1
545	40.621	1	9	88
546	40.697	9	1	1
547	40.773	5	4	110
548	40.848	4	5	1
549	40.924	15	6	89
550	41.000	6	15	1
551	41.076	3	8	119
552	41.152	8	3	1
553	41.227	7	11	77
554	41.303	11	7	2
555	41.379	7	15	19
556	41.455	15	7	2
557	41.531	7	6	19
558	41.606	6	7	2
559	41.682	18	1	94
560	41.758	1	18	1
561	41.834	1	9	2
562	41.909	9	1	1
563	41.985	12	10	112
564	42.061	4	5	52

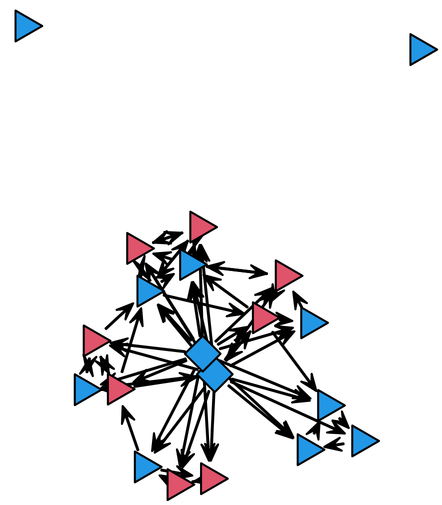
565	42.137	5	4	1
566	42.213	12	18	121
567	42.288	18	12	1
568	42.364	18	1	2
569	42.440	1	18	1
570	42.516	12	10	134
571	42.592	10	12	1
572	42.667	4	12	87
573	42.743	12	4	1
574	42.819	20	16	125
575	42.895	16	20	1
576	42.971	18	1	53
577	43.046	1	18	1
578	43.122	14	4	72
579	43.198	4	14	1
580	43.274	14	10	18
581	43.349	10	14	1
582	43.425	14	5	17
583	43.501	5	14	1
584	43.577	14	12	18
585	43.653	12	14	1
586	43.728	12	10	5
587	43.804	10	12	1
588	43.880	20	16	53
589	43.956	16	20	1
590	44.032	4	10	125
591	44.107	16	17	123
592	44.183	17	16	1
593	44.259	15	6	90
594	44.335	6	15	1
595	44.411	17	20	111
596	44.486	20	17	1
597	44.562	7	9	77
598	44.638	9	7	2
599	44.714	7	18	19
600	44.789	18	7	1
601	44.865	7	1	20
602	44.941	1	7	2
603	45.017	16	17	48
604	45.093	17	16	1
605	45.168	4	12	86
606	45.244	12	4	1
607	45.320	13	3	54
608	45.396	3	13	1
609	45.472	20	16	88
610	45.547	16	20	1
611	45.623	6	11	112
612	45.699	11	6	1
613	45.775	6	11	1
614	45.851	11	6	1
615	45.926	12	10	89
616	46.002	10	12	1
617	46.078	9	18	114
618	46.154	18	9	1

619	46.229	4	10	132
620	46.305	4	12	2
621	46.381	12	4	1
622	46.457	14	18	80
623	46.533	18	14	1
624	46.608	14	1	14
625	46.684	1	14	2
626	46.760	14	9	19
627	46.836	9	14	2
628	46.912	3	8	72
629	46.987	8	3	1
630	47.063	16	17	89
631	47.139	17	16	1
632	47.215	13	3	53
633	47.291	3	13	1
634	47.366	15	6	54
635	47.442	6	15	1
636	47.518	16	17	54
637	47.594	17	16	1
638	47.669	3	8	89
639	47.745	8	3	1
640	47.821	8	13	3
641	47.897	13	8	1
642	47.973	14	12	45
643	48.048	12	14	2
644	48.124	14	5	8
645	48.200	5	14	2
646	48.276	14	10	8
647	48.352	10	14	2
648	48.427	14	4	10
649	48.503	4	14	2
650	48.579	18	1	106
651	48.655	1	18	1
652	48.731	12	18	122
653	48.806	3	8	52
654	48.882	8	3	1
655	48.958	13	3	91
656	49.034	3	13	1
657	49.109	15	6	53
658	49.185	6	15	1
659	49.261	11	15	115
660	49.337	15	11	1
661	49.413	20	16	53
662	49.488	16	20	1
663	49.564	8	13	91
664	49.640	13	8	1
665	49.761	7	15	47
666	49.882	15	7	2
667	50.003	7	1	2
668	50.013	7	2	17
669	50.023	7	3	17
670	50.033	7	4	13
671	50.043	7	5	12
672	50.053	7	6	6

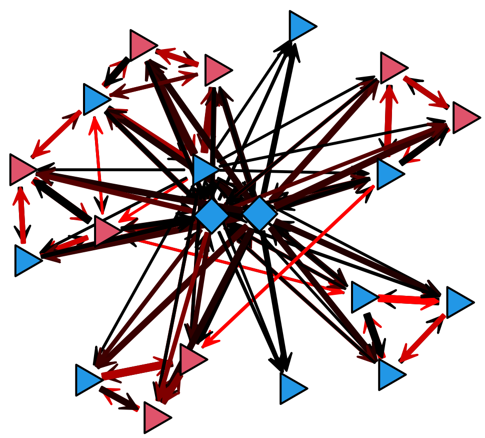
```
673     50.063     7    8                              13
674     50.073     7    9                               5
675     50.083     7   10                               9
676     50.093     7   11                               5
677     50.103     7   12                              10
678     50.113     7   13                              10
679     50.123     7   14                              19
680     50.133     7   15                               2
681     50.143     7   16                               8
682     50.153     7   17                               7
683     50.163     7   18                               4
684     50.173     7   19                              15
685     50.183     7   20                               8
686     50.304     1    7                              59
687     50.426     1    3                              22
688     50.547     3    1                               1
689     50.668     6   17                             142
690     50.789     6   17                             380
691     50.910    17    6                               1
692     50.920    NA   NA                              NA
```

It looks like there is some structure in the errors: we aren't able to capture certain kinds of intrusive events. Does looking at the "surprising" events (say, those for which the observed event is not in the top 5% of those predicted) in time-aggregate form help?

```
# Get the surprising events, and display as a network
surprising <- as.sociomatrix.eventlist(Class[classfit6$observed.rank >
   19, ], 20)
gplot(surprising, vertex.col = 4 - 2 * ClassIsFemale, vertex.sides = 3 +
   ClassIsTeacher, vertex.cex = 2)
```



```r
# Show how the 'surprising' events fit into the broader
# communication structure
edgecol <- matrix(rgb(surprising/(ClassNet + 0.01), 0, 0), 20,
   20)  #Color me surprised
gplot(ClassNet, edge.col = edgecol, edge.lwd = ClassNet^0.75,
   vertex.col = 4 - 2 * ClassIsFemale, vertex.sides = 3 + ClassIsTeacher,
   vertex.cex = 2)
```



The visualization gives us more of a clue about what we're missing: various side discussions occur that are not well-captured by the current model. This could be due to the fact that things like P-shift effects fail to capture simultaneous side conversations (each of which may have its own set of turn-taking patterns), or to a lack of covariates to capture the enhanced propensity of subgroup members to address each other. Further elaboration could be helpful here. On the other hand, we seem to be doing reasonably well at capturing the main line of discussion within the classroom, particularly vis a vis the instructors. Whether or not this is adequate depends on the purpose to which the model is to be put; as always, adequacy must be considered in light of specific scientific goals.

2.5 Simulating from the fitted model

Simulation from fitted models with exact timing proceeds exactly as in the ordinal timing case: we can use the `simulate` method for `rem.dyad` to generate trajectories from the fitted model object.

For instance, to generate a new trajectory from the final classroom model, we would use the code

```
set.seed(1331)
ClassSim <- simulate(classfit6, covar = list(CovSnd = cbind(ClassIntercept,
   ClassIsTeacher), CovRec = ClassIsTeacher))

ClassSim  #Examine the resulting trajectory
```

```
            [,1] [,2] [,3]
  [1,] 0.2452406    7    1
  [2,] 0.2648231    1    7
  [3,] 0.2823708    7   18
  [4,] 0.3090334   13   19
  [5,] 0.3387776    7    2
```

```
 [6,] 0.4176982  15  19
 [7,] 0.4333130  14  16
 [8,] 0.4465385  14  18
 [9,] 0.5291631  14   9
[10,] 0.6368674  14  10
[11,] 0.7403645  10  14
[12,] 0.8529576  14  18
[13,] 0.8781375  14  10
[14,] 0.9604438  14  12
[15,] 0.9896705  16  14
[16,] 0.9930157  14  16
[17,] 1.1128360   7   6
[18,] 1.1441811  14   7
[19,] 1.1651407  14   8
[20,] 1.1939772   8  14
[21,] 1.2091976  14   6
[22,] 1.2306047  14  17
[23,] 1.3323831  14  10
[24,] 1.3605220  10   5
[25,] 1.4054571   5  10
[26,] 1.4482527  10   5
[27,] 1.5010655  14   8
[28,] 1.5663907  14  16
[29,] 1.8808538  14  13
[30,] 2.0099635  14  19
[31,] 2.0260216  14  15
[32,] 2.1178520  14  18
[33,] 2.1972178  14  10
[34,] 2.2516805   7  14
[35,] 2.2757663   7  18
[36,] 2.2767540  17  19
[37,] 2.3050987  17  14
[38,] 2.3331962   7  20
[39,] 2.3480541   7  15
[40,] 2.4195505  15   7
[41,] 2.4486848   7  15
[42,] 2.5661515   7  19
[43,] 2.6034570   7  14
[44,] 2.6444055  14   7
[45,] 2.7902233   7  14
[46,] 2.8476529   7   4
[47,] 2.8892709   7   3
[48,] 2.8958928  13  16
[49,] 2.9141223  16  13
[50,] 3.2577775  13  16
[51,] 3.3103192  18   6
[52,] 3.6363817  17  20
[53,] 3.6689457  20  17
[54,] 3.6928119  20  10
[55,] 3.7176484  10  20
[56,] 3.8541742  20  10
[57,] 3.8883622  20   6
[58,] 3.9300445   6  20
[59,] 4.1380207  20   6
```

```
 [60,] 4.2587305  2  6
 [61,] 4.2860776  2  1
 [62,] 4.3805096 16  9
 [63,] 4.4431156 16 12
 [64,] 4.5267905 12 16
 [65,] 4.5635038 16 12
 [66,] 4.6236599 16  8
 [67,] 4.6471357  8 16
 [68,] 4.7474069 10 11
 [69,] 4.7939076 11 10
 [70,] 4.7961521  2 13
 [71,] 4.8091721 13  2
 [72,] 4.8247684 14 12
 [73,] 4.8955596 14 17
 [74,] 4.9081606 14  9
 [75,] 4.9153816 14 17
 [76,] 4.9806210 14  7
 [77,] 5.0242039 14  4
 [78,] 5.0613454  4 14
 [79,] 5.0644610 14  4
 [80,] 5.2103559 14  3
 [81,] 5.2849792 14  4
 [82,] 5.3802582 14 19
 [83,] 5.4723226 14  8
 [84,] 5.4730835 14  4
 [85,] 5.4856095  4 14
 [86,] 5.5160662 14  4
 [87,] 5.5235970  4 14
 [88,] 5.5503473  4 18
 [89,] 5.6166395 14 11
 [90,] 5.6329733 11 14
 [91,] 5.6923873 11  8
 [92,] 5.6942170  8 11
 [93,] 5.7328500 11  8
 [94,] 6.0436211 19 20
 [95,] 6.1846271  3 12
 [96,] 6.3465512  3 10
 [97,] 6.3948913 10  3
 [98,] 6.4390823 11 19
 [99,] 6.5775612 11  8
[100,] 6.7374425 11 14
[101,] 6.7471661 14 11
[102,] 6.9235061 14  2
[103,] 6.9321178 14 11
[104,] 7.0017914 14  7
[105,] 7.0218476 14  4
[106,] 7.1118430 10  2
[107,] 7.2821982  2 10
[108,] 7.2954398  2  5
[109,] 7.4197377  2 13
[110,] 7.5068005 19 13
[111,] 7.5149229 13 19
[112,] 7.5259535 13 17
[113,] 7.5536580 17 13
```

```
[114,]  7.6412618   14    9
[115,]  7.6970685   14   11
[116,]  7.7209054   14    4
[117,]  7.7972795   14   17
[118,]  7.8557384   14   11
[119,]  7.8695549   14   13
[120,]  7.8987990    4    8
[121,]  7.9182603   20   15
[122,]  7.9188059   20   19
[123,]  7.9489409   19   20
[124,]  8.1252133   20   19
[125,]  8.1253137   12    1
[126,]  8.1870938    7   14
[127,]  8.2255444    6   13
[128,]  8.2850498   13    6
[129,]  8.3191521   13    1
[130,]  8.3472563   13   11
[131,]  8.4147805   11   13
[132,]  8.5221672   13   15
[133,]  8.5532448   15   13
[134,]  8.6039365    9    2
[135,]  8.6043771    2    9
[136,]  8.6103668   15   13
[137,]  9.1065793   10   11
[138,]  9.1890090   11    9
[139,]  9.1973022   10   20
[140,]  9.2939096   14    3
[141,]  9.4186345    3   14
[142,]  9.4677800   14    3
[143,]  9.5318442   11   10
[144,]  9.6027641    8    4
[145,]  9.6083736   14   10
[146,]  9.6511044   10   14
[147,]  9.6585089   14   10
[148,]  9.6731494   14    3
[149,]  9.7398523   14   10
[150,]  9.7956552   14    3
[151,]  9.9224096   17   10
[152,]  9.9843138   10   17
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[154,] 10.2442880    4    8
[155,] 10.5105997    4   14
[156,] 10.5192640   14    4
[157,] 10.5904990   14    5
[158,] 10.6502651    4    8
[159,] 10.7461853   11   17
[160,] 10.7516434   17   11
[161,] 10.7689437    2    6
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As we saw in section 1.5, running the `simulate` command on the fitted model object produces a new trajectory of identical length to the original, with the same coefficients. Note that the new trajectory is identical in terms of the number of *realized events* it contains, and it will not in general cover the same *time period.* Some disparity between the two is normal (and, indeed, will happen with probability 1); however, when the total mean time period of the replicate sequences is substantially different from that of the original data, this suggests that the pacing of the model is off.

In section 1.5, we showed how an *in silico* knock-out study could be used to gain insights into model behavior. Another useful strategy can be to simulate trajectories from a fitted model with alternative choices of covariates. For instance, what might we expect if we replaced the teachers in our classroom with students? This anarchic state of affairs can be probed by conditional simulation with a different set of covariates:

```r
set.seed(1331)
AnarchSim <- simulate(classfit6, covar = list(CovSnd = cbind(ClassIntercept,
   rep(0, 20)), CovRec = rep(0, 20)))

AnarchSim  #Examine the trajectory
```

```
             [,1] [,2] [,3]
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  [9,] 0.6802183    2    9
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[519,] 41.6023613   15   16
[520,] 41.6068314    2    3
[521,] 41.7873260    3    2
[522,] 41.9382777    2    3
[523,] 41.9569746    3    2
[524,] 41.9728778    2    3
[525,] 41.9750713    2    9
[526,] 42.0204511    9    2
[527,] 42.1750867    9    3
[528,] 42.2161147    3    9
[529,] 42.2297397    9    3
[530,] 42.3255960    5    3
[531,] 42.4227911    5   10
[532,] 42.4676809   14    5
[533,] 42.5329359   11   13
```

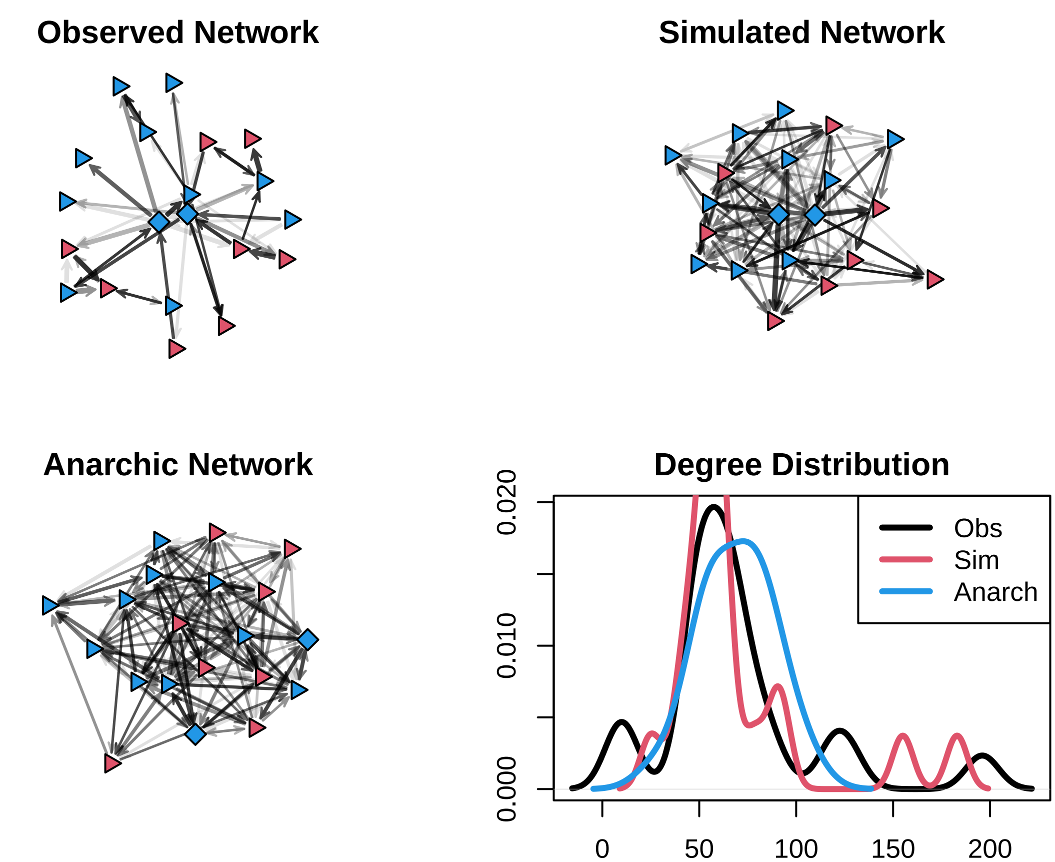
```
[534,] 42.5701089   13   11
[535,] 42.6716845    8    7
[536,] 42.6900568    7    8
[537,] 42.8975914    7   13
[538,] 42.9325214   13    7
[539,] 42.9428758    6   16
[540,] 42.9548842    5   14
[541,] 43.0042786    5   11
[542,] 43.0992647   11    5
[543,] 43.1257381   16    6
[544,] 43.3891977    4   16
[545,] 43.4003161    4    2
[546,] 43.4955178    2    4
[547,] 43.5399652    2   19
[548,] 43.5958527   19    2
[549,] 43.6702128    2   18
[550,] 43.7902078   18    2
[551,] 43.8254534   18    9
[552,] 43.8834585    9   18
[553,] 44.0695929   18    9
[554,] 44.5836345   18    4
[555,] 44.8796521    3    8
[556,] 44.9155000    8    3
[557,] 44.9606795    8   12
[558,] 45.0085411   12    8
[559,] 45.0745201    8   12
[560,] 45.0823571   16    4
[561,] 45.0871409    4   16
[562,] 45.0911252   15    2
[563,] 45.1867028    3    8
[564,] 45.2768829    4    6
[565,] 45.4789807    6    4
[566,] 45.4900682    6    7
[567,] 45.5039850    7    6
[568,] 45.5497765    6    7
[569,] 45.6029949    6   10
[570,] 45.6056295    6    4
[571,] 45.6588613   18    7
[572,] 45.6611039   15   13
[573,] 45.7027269   15   18
[574,] 45.7053350   18   15
[575,] 45.7674247   15   18
[576,] 45.8020391   15    5
[577,] 46.0778106    5    6
[578,] 46.1071622    6    5
[579,] 46.1080589    5    6
[580,] 46.1490436   10    6
[581,] 46.1691319   19    2
[582,] 46.3703765    8    7
[583,] 46.4071231    8   10
[584,] 46.5030231   16    8
[585,] 46.5363165    8   16
[586,] 46.6442121    8    5
[587,] 46.6444168   20    7
```

[588,]	46.6501200	7	20
[589,]	46.7511316	20	7
[590,]	46.7967767	7	20
[591,]	46.8288981	7	8
[592,]	46.9395512	2	1
[593,]	46.9759281	1	2
[594,]	47.0500484	1	16
[595,]	47.1180004	1	5
[596,]	47.1806417	5	1
[597,]	47.4092114	8	19
[598,]	47.6157842	17	8
[599,]	47.6426026	8	17
[600,]	47.6964853	17	4
[601,]	47.7540529	4	17
[602,]	47.8678685	4	10
[603,]	47.8746077	4	6
[604,]	47.8832622	6	4
[605,]	47.9066844	6	7
[606,]	47.9103155	6	4
[607,]	47.9486072	4	2
[608,]	48.1365235	2	4
[609,]	48.1615780	4	3
[610,]	48.1816496	16	4
[611,]	48.2445358	11	5
[612,]	48.3090376	5	11
[613,]	48.3689472	19	6
[614,]	48.3796791	6	19
[615,]	48.3811114	6	8
[616,]	48.5046934	8	6
[617,]	48.8089886	9	10
[618,]	48.8142084	10	9
[619,]	48.9103383	10	4
[620,]	49.1905268	4	10
[621,]	49.3159817	4	20
[622,]	49.3286881	13	10
[623,]	49.3390245	10	13
[624,]	49.3495440	10	8
[625,]	49.5351129	10	14
[626,]	49.5702665	14	7
[627,]	49.6859966	14	5
[628,]	49.8167083	7	18
[629,]	49.8387285	7	13
[630,]	49.8805012	7	14
[631,]	49.9559317	14	7
[632,]	50.0062988	7	18
[633,]	50.0250681	18	7
[634,]	50.0444724	14	7
[635,]	50.0571854	8	11
[636,]	50.0872506	8	6
[637,]	50.1239492	9	6
[638,]	50.1352551	6	9
[639,]	50.1475510	6	10
[640,]	50.2100534	12	16
[641,]	50.2296226	16	12

```
[642,] 50.7118727    7   14
[643,] 51.0499391   14    7
[644,] 51.1000967    6    9
[645,] 51.1030595    9    6
[646,] 51.3225780    8   16
[647,] 51.3644111   16    8
[648,] 51.5621604    8   16
[649,] 51.6605795   16    8
[650,] 51.8078117   16    6
[651,] 51.9342197    6   16
[652,] 52.1516087   10    6
[653,] 52.4184928   10   20
[654,] 52.6962118   16    7
[655,] 52.7799093    7   16
[656,] 52.8842754   15   17
[657,] 52.9440578   17   15
[658,] 53.0165125    7   16
[659,] 53.2153132   17   18
[660,] 53.2226518    3   20
[661,] 53.3076277   20    3
[662,] 53.3533058    3   20
[663,] 53.3665635   20    6
[664,] 53.6463135    6   20
[665,] 53.6742425   18   17
[666,] 53.9752778   17   18
[667,] 54.1710773    9    2
[668,] 54.3845464    9   18
[669,] 54.4013738    9   12
[670,] 54.6077034   12    9
[671,] 54.7498754    5   16
[672,] 54.7642237    5    6
[673,] 54.9593488    5   20
[674,] 55.0086062   20    5
[675,] 55.0592746    5   20
[676,] 55.0985405    5    9
[677,] 55.1086941    9    5
[678,] 55.1268444   11    9
[679,] 55.1827019    9   11
[680,] 55.1974932   11    9
[681,] 55.2493971    9   15
[682,] 55.3385465    9    6
[683,] 55.4786241    6    9
[684,] 55.5277270    9    6
[685,] 55.8172419    9    4
[686,] 55.9024692    4    9
[687,] 55.9679248    4    6
[688,] 55.9698699    4    9
[689,] 56.0101293    4    6
[690,] 56.0193832    4   16
[691,] 56.1502882    4   18
[692,] 56.4316135   18    4
attr(,"n")
[1] 20
```

```r
# Plot the network structure of the simulations, and the
# observed data
par(mfrow = c(2, 2), mar = c(2, 2, 2, 2))
gplot(ClassNet, vertex.col = 4 - 2 * ClassIsFemale, vertex.sides = 3 +
   ClassIsTeacher, vertex.cex = 2, edge.lwd = ClassNet^0.75,
   main = "Observed Network", edge.col = rgb(0, 0, 0, (1 - 1/(1 +
      ClassNet))^3))
SimNet <- as.sociomatrix.eventlist(ClassSim, 20)  #Create a network from the fitted sim
gplot(SimNet, vertex.col = 4 - 2 * ClassIsFemale, vertex.sides = 3 +
   ClassIsTeacher, vertex.cex = 2, edge.lwd = SimNet^0.75, main = "Simulated Network",
   edge.col = rgb(0, 0, 0, (1 - 1/(1 + SimNet))^3))
AnarchNet <- as.sociomatrix.eventlist(AnarchSim, 20)  #Create a network from the anarchy sim
gplot(AnarchNet, vertex.col = 4 - 2 * ClassIsFemale, vertex.sides = 3 +
   ClassIsTeacher, vertex.cex = 2, edge.lwd = AnarchNet^0.75,
   main = "Anarchic Network", edge.col = rgb(0, 0, 0, (1 - 1/(1 +
      AnarchNet))^3))

# Plot the valued degree distributions
plot(density(degree(ClassNet), bw = "SJ"), lwd = 3, main = "Degree Distribution")
lines(density(degree(SimNet), bw = "SJ"), lwd = 3, col = 2)
lines(density(degree(AnarchNet), bw = "SJ"), lwd = 3, col = 4)
legend("topright", legend = c("Obs", "Sim", "Anarch"), lwd = 3,
   col = c(1, 2, 4))
```



Comparing the plots, we can see several things. First, we note some limitations of our fitted model: while it does relatively well at ensuring that the teachers are central, enduring that many of the strongest interactions are student-teacher interactions, creating a network in which strong interactions are localized to a fairly small number of (highly reciprocal) dyads, and reproducing the overall valued degree distribution, it also produces a large "halo" of weak side-interactions among the students that is not seen in the observed network. This suggests the potential for further model improvement.

Turning to our "anarchy in the classroom" model, however, we see that the effect of removing teachers is substantively reasonable. The nodes that were formerly teachers no longer have any particular significance, and are now well-mixed with their peers; likewise, without the teachers to focus attention, the network is as a whole much less centralized. Thus, the model does plausibly produce many of the effects one would expect to see from such a change in group composition. Such scenario-based probes can be a useful tool for assessing model behavior, as well as being of possible substantive interest in and of themselves.

Section 3. Simulating *De Novo* Dyadic Relational Event Models

We have seen how the `simulate` command can be used to simulate draws from fitted `rem.dyad` objects, and even how these may be modified by switching coefficients or covariates for particular purposes. What if we want to create a *de novo* simulation? This can also be done, using `rem.dyad` to create a *model skeleton* that can subsequently be used for simulation.

3.0 Creating a model skeleton

To set up a REM for simulation, we need to create an object that records the system size (i.e., number of vertices), effects involved, and other critical information. When we fit models using 'rem.dyad'', this information was encoded in the model object. In the *de novo* case, we use the same approach - except that we simply omit the data!

To see how this is done, let's consider an example. Let us say that we want to create a model for a 25-node REM with a baseline intercept, an AB-BA P-shift, and a recency effect of sending on future sending (`RSndSnd`). We then proceed by creating a model just as we would normally, but with `NULL` where the data should be:

```
ModInt <- rep(1, 25)
modskel <- rem.dyad(NULL, n = 25, effects = c("CovSnd", "PSAB-BA",
   "RSndSnd"), covar = list(CovSnd = ModInt))
```

```
NULL edgelist passed to rem.dyad - creating model skeleton.
Checking/prepping covariates.
```

```
modskel
```

```
Relational Event Model
    Model skeleton (not fit)

Embedded coefficients:
      RSndSnd      CovSnd.1        PSAB-BA
 0.0007478403 -0.0007507346  0.0011755427
```

Note that the model is correctly identified as a skeleton, with a reminder that it was not fit to data. It also comes equipped with "default" coefficients, but these are not very useful: if a seed coefficient is not passed, `rem.dyad` always initializes with perturbed coefficients near zero. If one knows what coefficients one wants to embed in the skeleton, one can set them using the `coef.seed` argument.

Note that none of the inferential or other arguments to `rem.dyad` are needed here, since no fitting is done. Perhaps less obviously, we do not need to set the `ordinal` variable, since all REM simulation is done in continuous time. (The resulting trajectories can, of course, be interpreted ordinally, if the pacing constant used was arbitrary.)

3.1 Simulating from the model skeleton

Simulation from the model skeleton is then performed just as simulation with fitted model objects, except that one needs to pass the number of draws to take (`nsim`, which was optional before) and `coef` (unless one already embedded the coefficients one wants in the model object). Be sure to enter your coefficients in the order stored in the skeleton, which may not be the order you initially specified the effects! Let's see how this works, using our example:

```
set.seed(1331)
modsim <- simulate(modskel, nsim = 100, coef = c(0.25, -1, 4),
   covar = list(CovSnd = ModInt))
head(modsim)  #See the trajectory
```

```
            [,1] [,2] [,3]
[1,] 0.003446229   20    2
[2,] 0.004616100    9    6
[3,] 0.005879407   25   17
[4,] 0.007751835   10   23
[5,] 0.009434835    9   20
[6,] 0.015124865   14   23
```

```
grecip(as.sociomatrix.eventlist(modsim, 25), measure = "edgewise")  #Relatively reciprocal
```

```
      Mut
0.2444444
```

Any number of events may be simulated in this way.

3.2 Simulation with time-varying covariates

Time-varying covariates must, by definition, be specified at each time step. `rem.dyad` understands several covariate formats (see `?rem.dyad`):

- Single covariate, time invariant: For `CovSnd`, `CovRec`, or `CovInt`, a vector or single-column matrix/array. For `CovEvent`, an `n` by `n` matrix or array.
- Multiple covariates, time invariant: For `CovSnd`, `CovRec`, or `CovInt`, a two-dimensional `n` by `p` matrix/array whose columns contain the respective covariates. For `CovEvent`, a `p` by `n` by `n` array, whose first dimension indexes the covariate matrices.
- Single or multiple covariates, time varying: For `CovSnd`, `CovRec`, or `CovInt`, an `m` by `n` by `p` array whose respective dimensions index time (i.e., event number), covariate, and actor. For `CovEvent`, a `m` by `p` by `n` by `n` array, whose dimensions are analogous to the previous case.

Thus, in the time-varying case, the dimensions of the covariate object must be consistent with `nsim`. Let's see a simple example, involving a 10-person group with an initial activity covariate that decays with time. We will simulate for 100 time steps, so need to create a 100 by 1 by 10 matrix to hold the covariate (the ith slice containing the covariate values "going into'' the ith event). When creating the skeleton, it is currently necessary to pass covariates as if they are static, since there are not yet multiple time points; the checks that are performed to ensure that the covariates are legal will object if too many time points are given. (This will probably change in the future.) The time-varying version is then passed to the simulator.

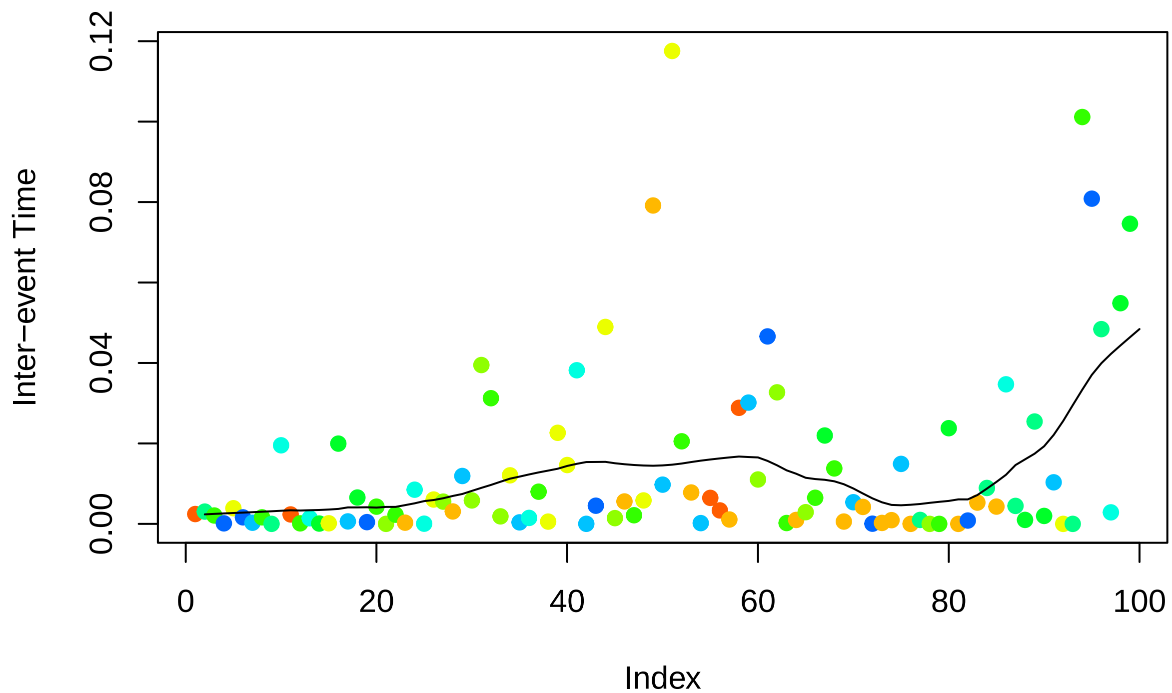
```
set.seed(1331)
# Set up the model
tcovar <- array(sweep(sapply(1:10, rep, 100), 1, 1/1.05^(0:99),
   "*"), dim = c(100, 10, 1))
SndInt <- rep(1, 10)
# Note that, in making the skeleton, we need to pass the
# covariates as if they are static - that's because the
# model doesn't contain time points yet.
```

```r
modskel2 <- rem.dyad(NULL, n = 10, effects = c("CovSnd", "CovInt"),
   coef.seed = c(-1, 1), covar = list(CovSnd = SndInt, CovInt = tcovar[1,
      , 1]))
```

```
NULL edgelist passed to rem.dyad - creating model skeleton.
Checking/prepping covariates.
```

```r
# Simulate draws
modsim2 <- simulate(modskel2, nsim = 100, covar = list(CovSnd = SndInt,
   CovInt = tcovar))

# Note that dynamics slow down, and participation evens out
plot(diff(modsim2[, 1]), col = hsv(modsim2[, 2]/10 * 0.6), pch = 19,
   ylab = "Inter-event Time")
lines(supsmu(x = 2:100, y = diff(modsim2[, 1])))
```



On average, dynamics slow down, as we would expect, and more low-numbered (redder) vertices interact after the initial period.

References

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